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# Modeling of Modes Competition and Thermal Effects in Large Mode Area Photonic Crystal Fibers

C. Molardi, F. Poli, A. Cucinotta, S. Selleri

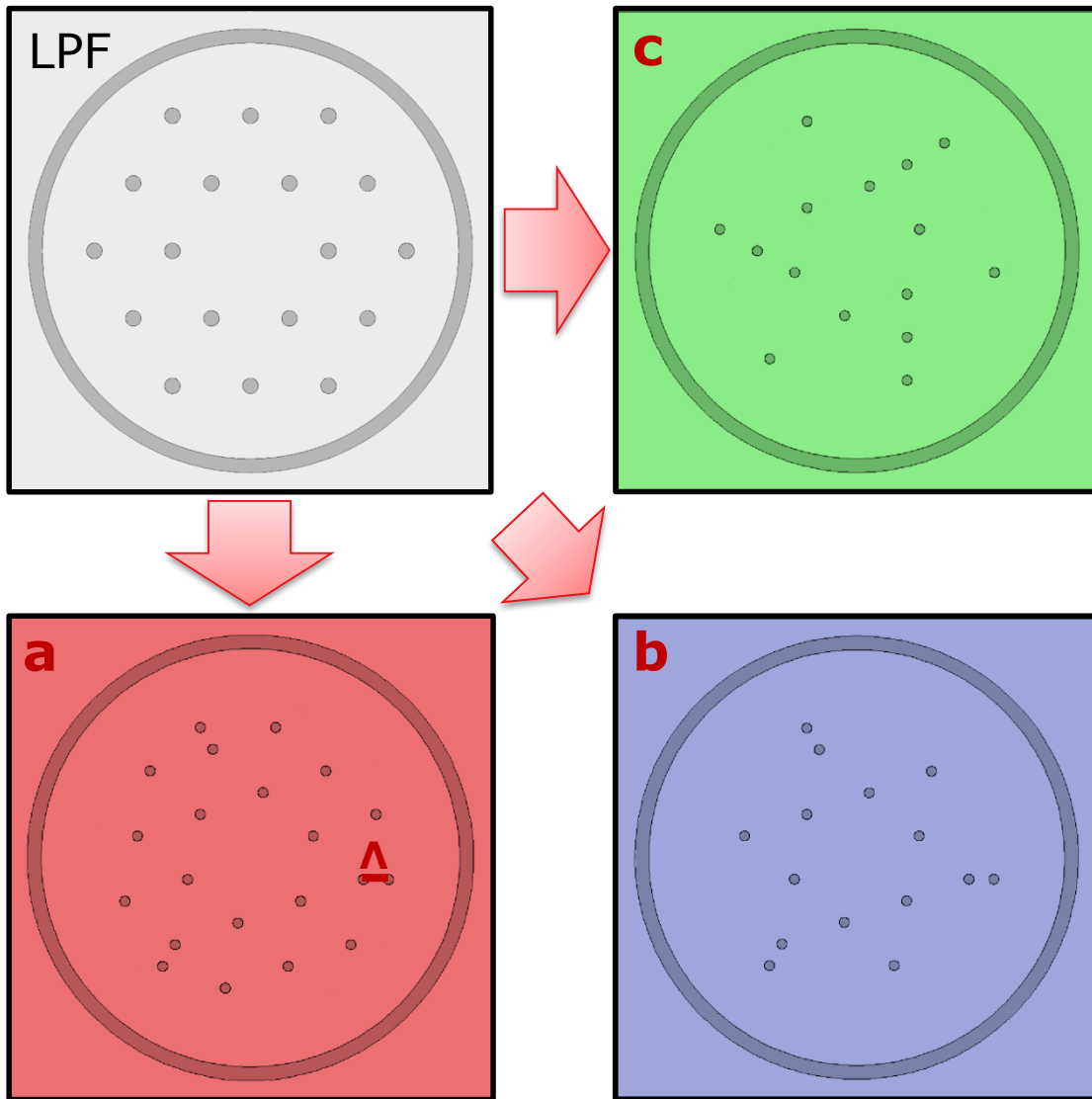
EAGLES

International Conference on  
Rare-Earth Doped Glass Materials and Fibre Lasers

Trento, 18-19 October 2016

- New designs of large mode area Yb-doped fibers without symmetry in the inner cladding
- Numerical simulations:
  - Modal analysis
  - Thermal effect model
- Study of the thermal effect influence on:
  - Single mode behavior
  - Effective area
- New model to describe z-variation
- Conclusion

# Reduced symmetry PCFs



**Idea:** remove mirror symmetry of the cladding to enhance delocalization of  $LP_{11}$  mode

- 19-cell hexagonal core (edge of  $36\text{ }\mu\text{m}$ )
- Air-hole diameter:  $d = 5.76\text{ }\mu\text{m} = 0.4\Lambda$
- Pitch:  $\Lambda = 14.4\text{ }\mu\text{m}$
- Inner cladding radius:  $120\text{ }\mu\text{m}$
- Air-cladding width:  $8\text{ }\mu\text{m}$

Fundamental Mode (**FM**) and first  $LP_{11}$ -like Higher-Order Modes (**HOM** =  $HOM_{1x, x=1...4}$ ) at 1032 nm

Overlap integral  $\Gamma$  on the hexagonal doped core calculated to evaluate the mode confinement:

$$\Gamma = \iint_S i(x, y) dx dy$$

S: hexagonal core  
 $i(x, y)$ : normalized intensity

- Differential overlap  $\Delta\Gamma$  (overlap difference between FM and HOM) considered to define the Single Mode (**SM**) region:

$$\Delta\Gamma > 0.3$$

- FM tight confinement ( $\Gamma > 0.8$ ) required in the SM region

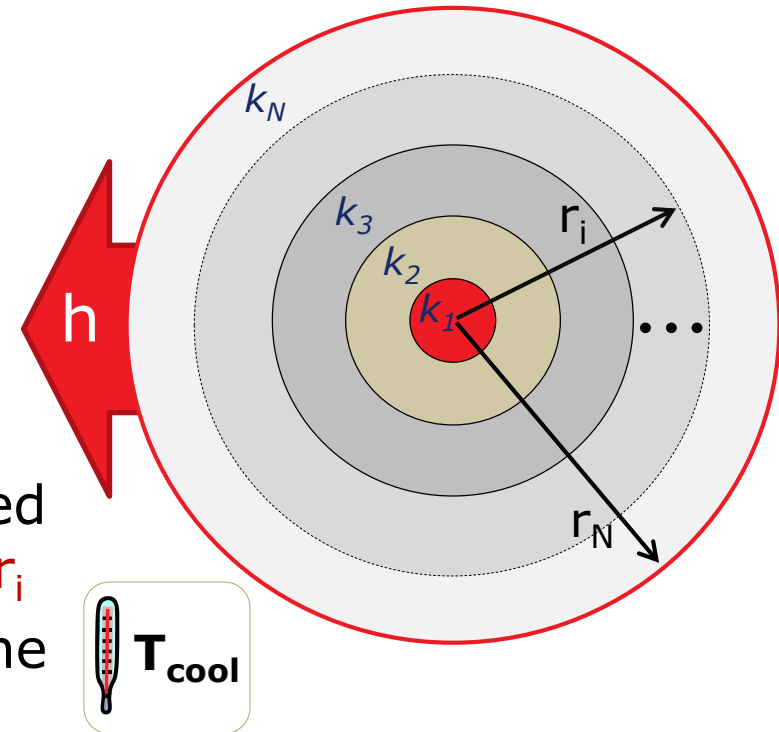
Effective area  $A_{\text{eff}}$  evaluated to study the influence of thermal lensing on the FM confinement

# Thermal effect model

- Heat generation
- Temperature gradient  $\Delta T$
- Refractive index change  $\Delta n = \beta \cdot \Delta T$ ,  
 $\beta = 1.16 \cdot 10^{-5} \text{ 1/K}$  for silica

New guiding properties



- PCF section: different rings, described by thermal conductivity  $k_i$  and radius  $r_i$
- Heat density  $Q_0$  generated into the doped core
- Convection cooling, described by convection coefficient  $h$ , at the outer surface

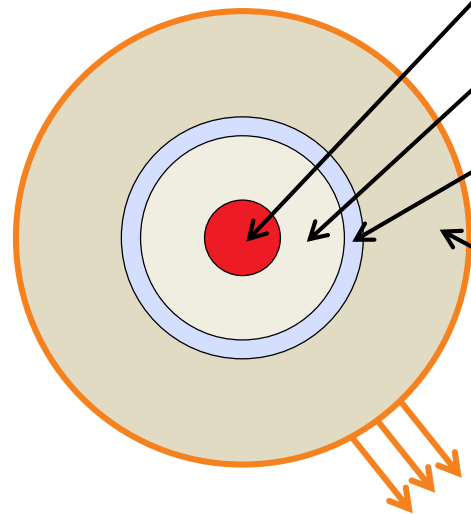


- $k_1, \dots, k_N$ : thermal conductivity (silica:  $1.38 \text{ W/(m}\cdot\text{K)}$ )
- $r_1, \dots, r_N$ : external radius
- $T_{\text{cool}}$ : outer temperature

E. Coscelli et al, Journal of Lightwave Technology, Vol. 30, pp. 3494-3499 (2012)

## Fiber cross-section characteristics

 Silica  
 Air-clad



**Core:**  $r_1 = 32.74 \mu\text{m}$ ,  $k_1 = 1.38 \text{ W/(m K)}$

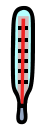
**Inner cladding:**  $r_2 = 120 \mu\text{m}$ ,  
 $k_2 = 1.38 \text{ W/(m}\cdot\text{K)}$

**Air cladding\*:**  $r_3 = 128 \mu\text{m}$   
 $n = 111$ ,  $b = 0.35 \mu\text{m}$   
 $k_{\text{air}} = 0.023 \text{ W/(m}\cdot\text{K)}$   
 $k_{\text{silica}} = 1.38 \text{ W/(m}\cdot\text{K)}$

$k_{\text{eq}} = 0.0918 \text{ W/(m}\cdot\text{K)}$

**Outer cladding:**  $r_4 = 850 \mu\text{m}$ ,  $k_4 = 1.38 \text{ W/(m}\cdot\text{K)}$

**Convection cooling:**  $h = 80 \text{ W/(K}\cdot\text{m}^2)$  (air flow)



$T_{\text{cool}} = 298.15 \text{ K}$

**\*air-cladding equivalent thermal conductivity:**

$$k_{eq,AC} = k_{air} + \frac{n \cdot b \cdot k_{silica}}{2\pi(r_3 - r_2)} \ln\left(\frac{r_3}{r_2}\right)$$

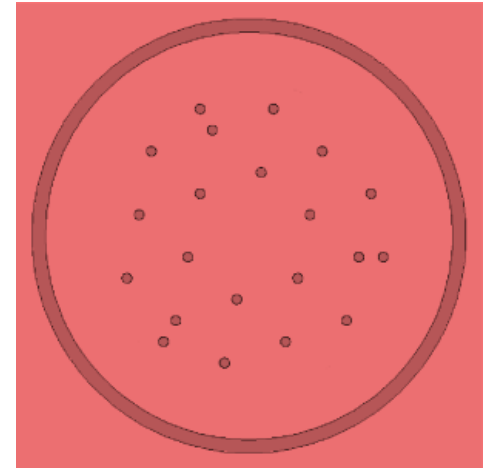
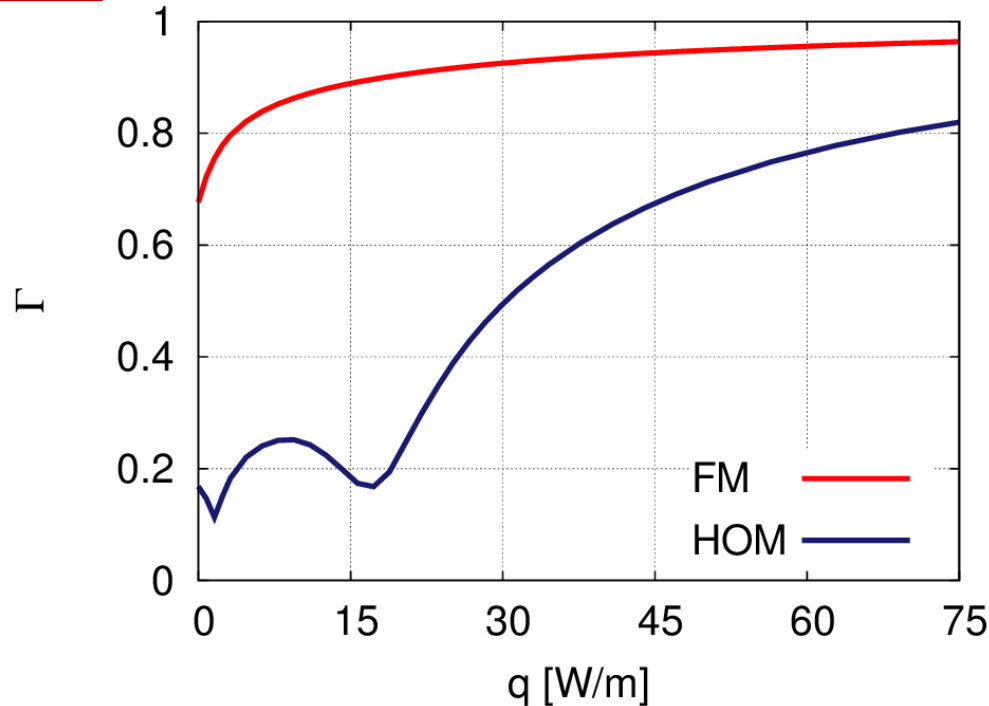
- Quantum defect-generated heat density  $Q_0$
- $Q_0 = q/A_{\text{core}}$   
 $q$ : heat load per unit length (W/m)  
 $A_{\text{core}}$ : core doped area

Generated heat due to pump conversion

$$q = \frac{1 - 10^{-\alpha \frac{dL}{10}}}{dL} \left( 1 - \frac{\lambda_p}{\lambda_s} \right) P$$

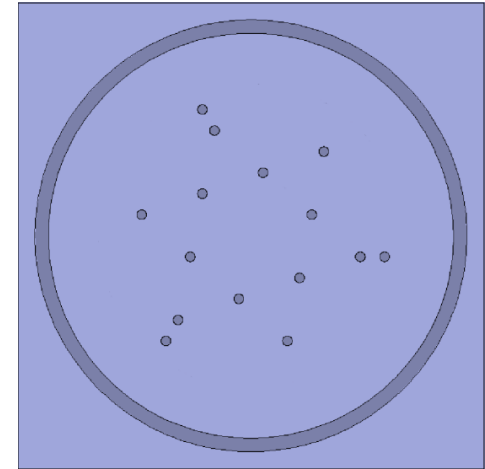
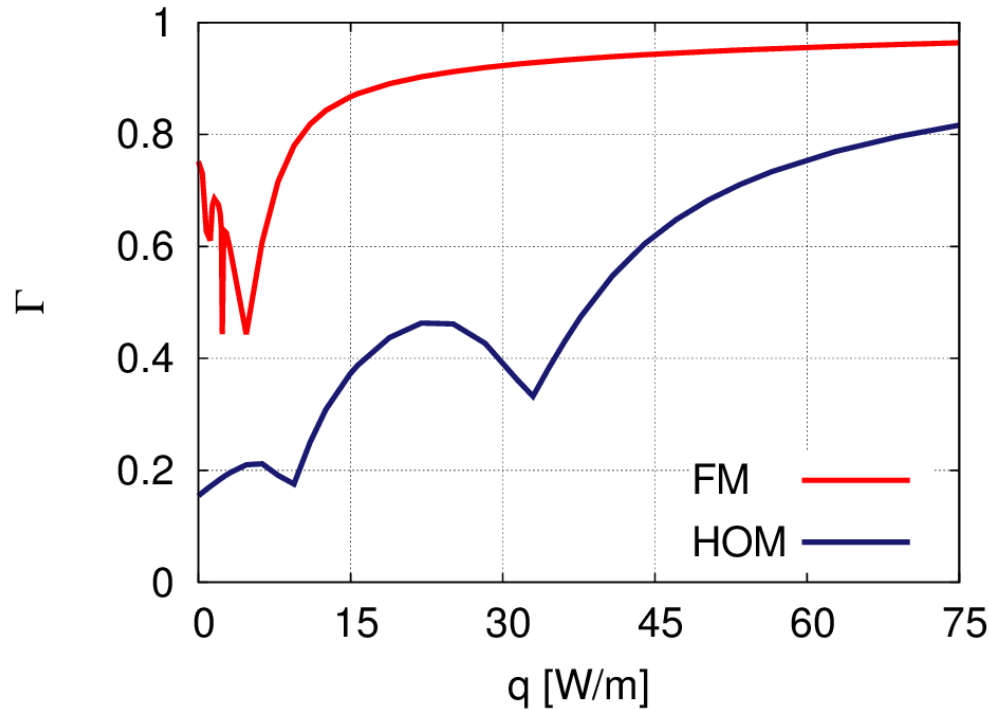
$\alpha$	Pump absorption	27 dB/m
$dL$	Fiber length over which average heat load is calculated	0.1 m (close to pumping end)
$\lambda_p$	Pump wavelength	976 nm
$\lambda_s$	Signal wavelength	1032 nm
$P$	Pump power	0 – 300 W

$$\lambda = 1032 \text{ nm}$$



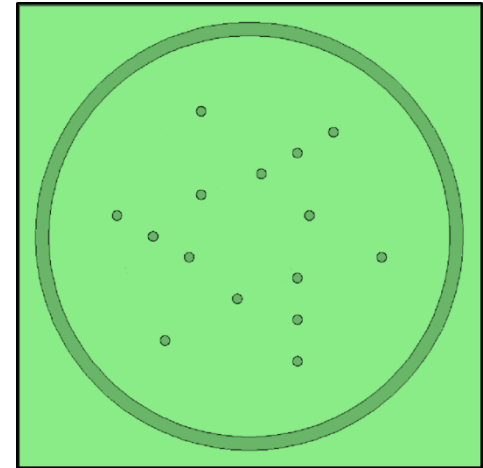
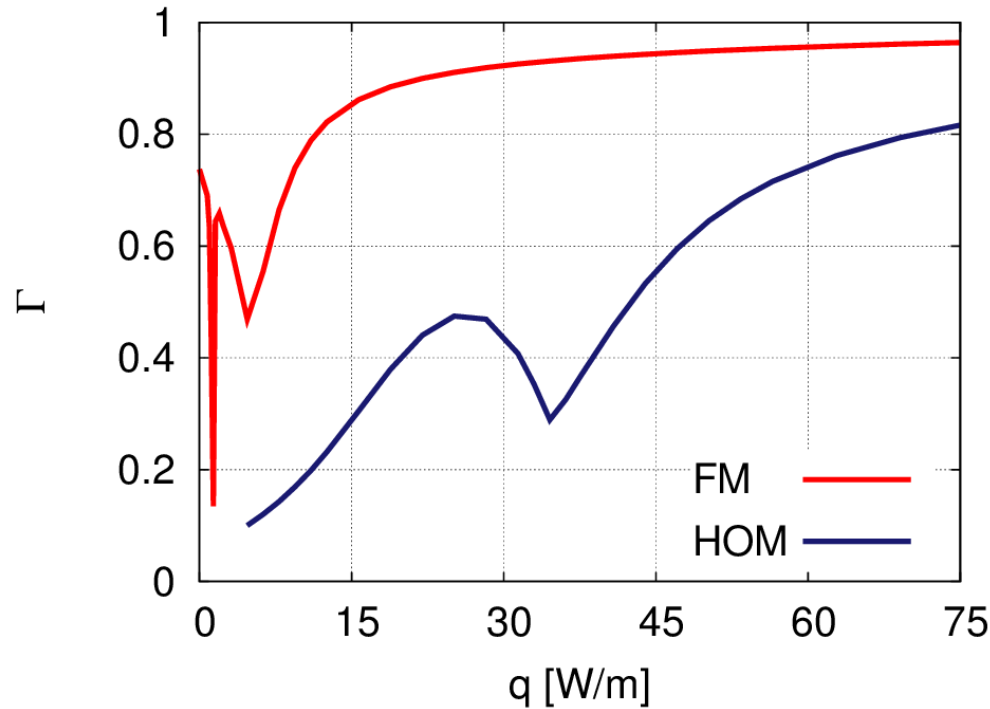
- FM well confined ( $\Gamma \geq 0.8$ ) for  $q \geq 3.9 \text{ W/m}$ , and guided even without pumping ( $\Gamma \approx 0.68$  in the “cold” fiber)
- HOM poorly guided for low  $q$  values, with significant field in the inner cladding, and better confinement as  $q$  increases
- Different HOM solutions due to coupling with cladding modes

$$\lambda = 1032 \text{ nm}$$



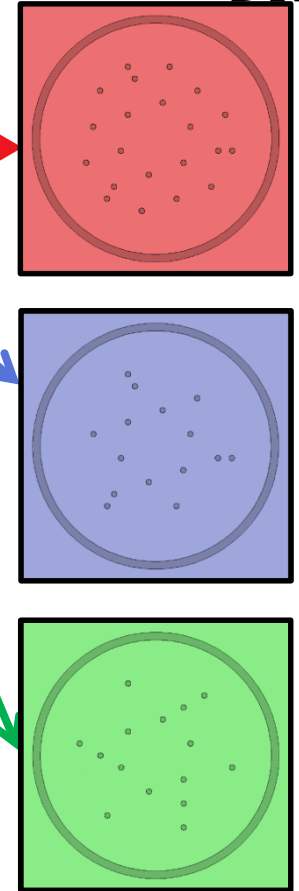
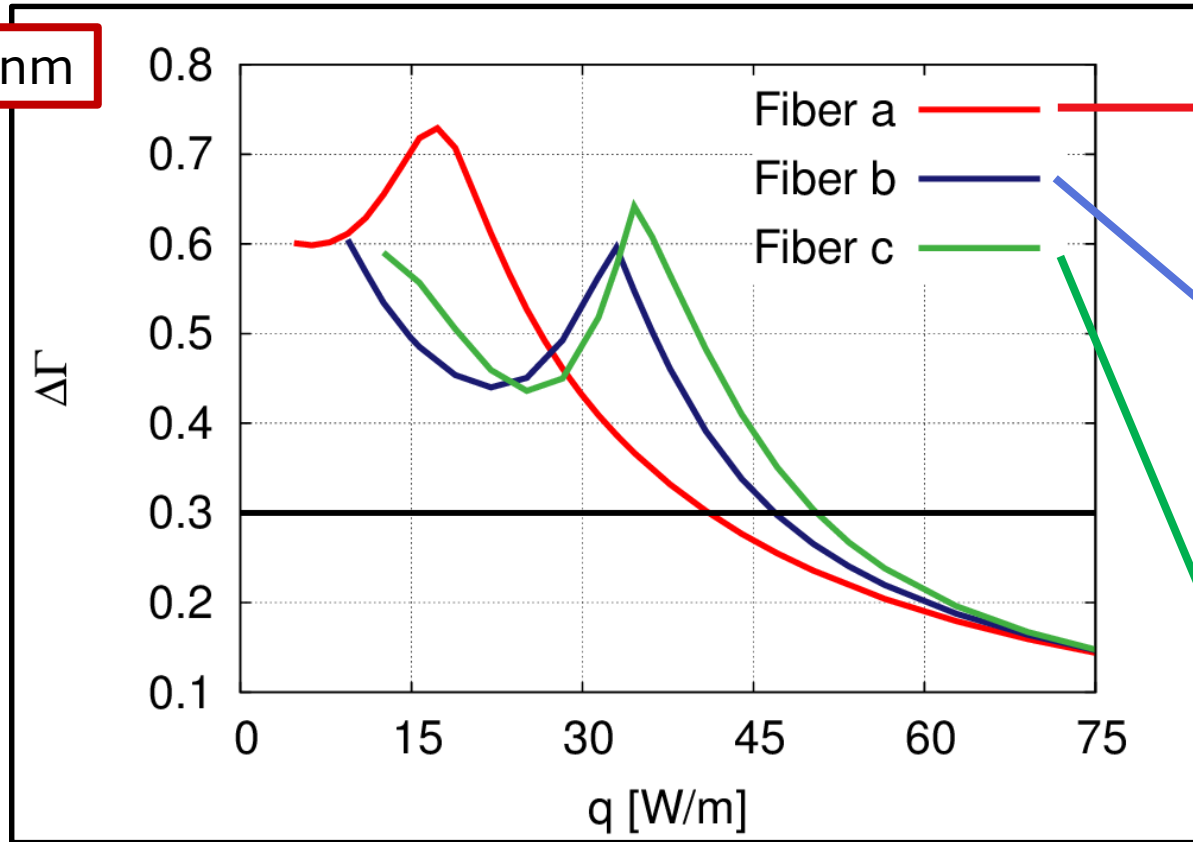
- FM not truly guided in the “cold” fiber and for low pump power values (effective refractive index difference not enough), and well confined ( $\Gamma \geq 0.8$ ) for  $q \geq 8.6$  W/m
- Different HOMs, coupled to cladding modes, for  $q \leq 32$  W/m
- Tighter FM and HOM confinement as  $q$  increases

$\lambda = 1032 \text{ nm}$



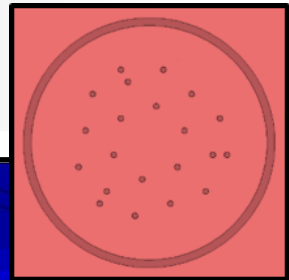
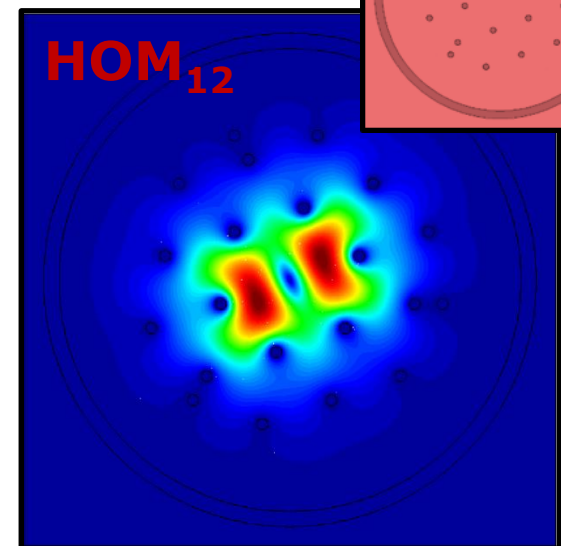
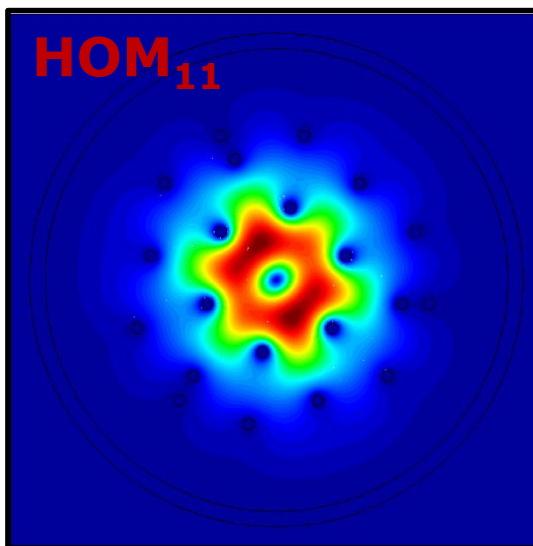
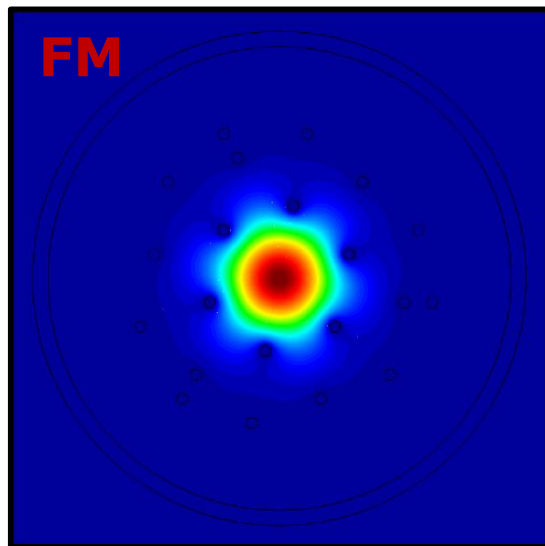
- FM and HOM poorly guided for low pump power values, with significant field distribution in the inner cladding (unwanted coupling with cladding modes)
- Better confinement of both modes as  $q$  increases
- FM well confined ( $\Gamma \geq 0.8$ ) for  $q \geq 11 \text{ W/m}$

$$\lambda = 1032 \text{ nm}$$

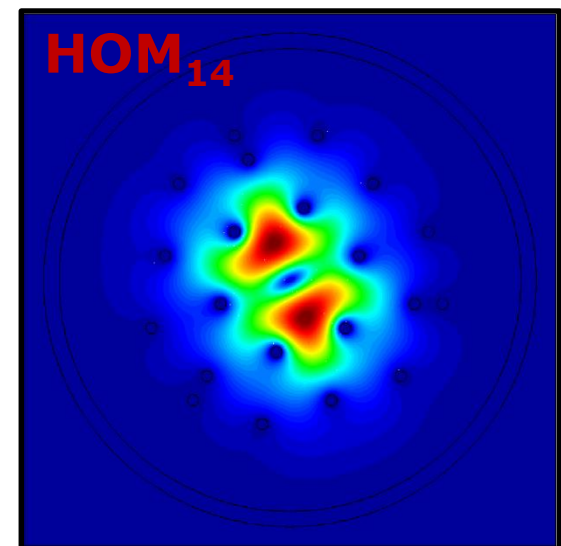
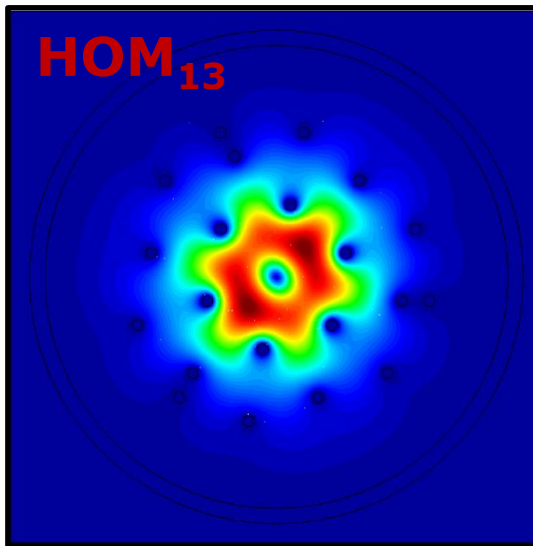


- **Fiber c** SM range similar to the **Fiber b** one, only slightly shifted towards higher  $q$  values ( $q$  between 11  $\text{W/m}$  and 50  $\text{W/m}$ )
- Only **Fiber a** is SM for low heat load values
- Higher  $q$  values ( $\approx 50 \text{ W/m}$ ) reached by **Fiber b** and **c** with SM behavior

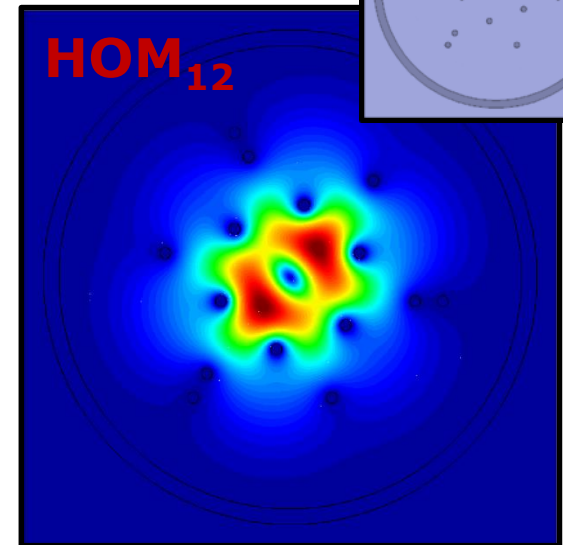
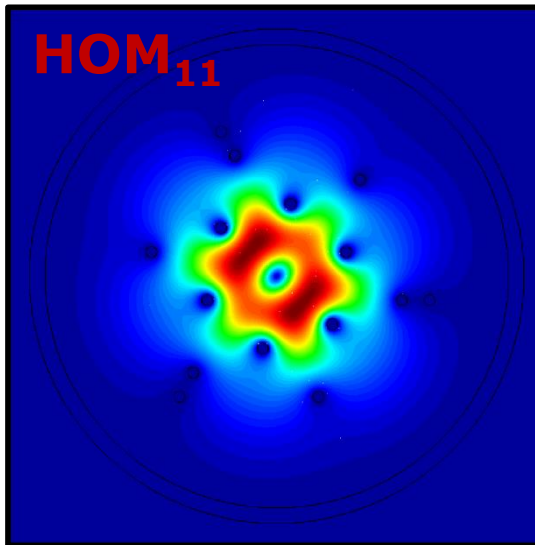
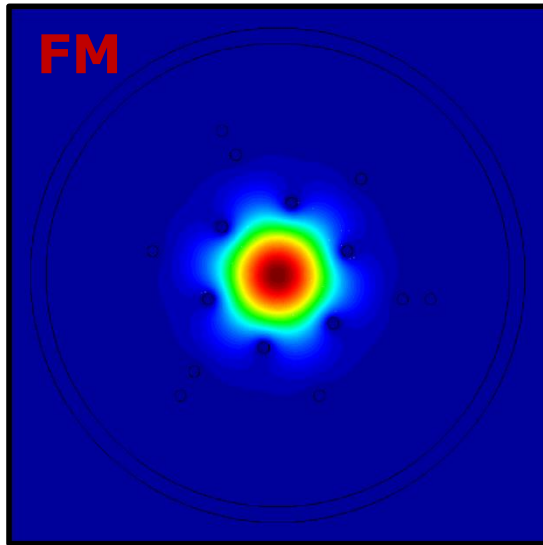
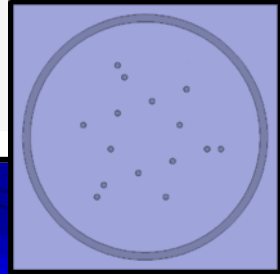
# Fiber a



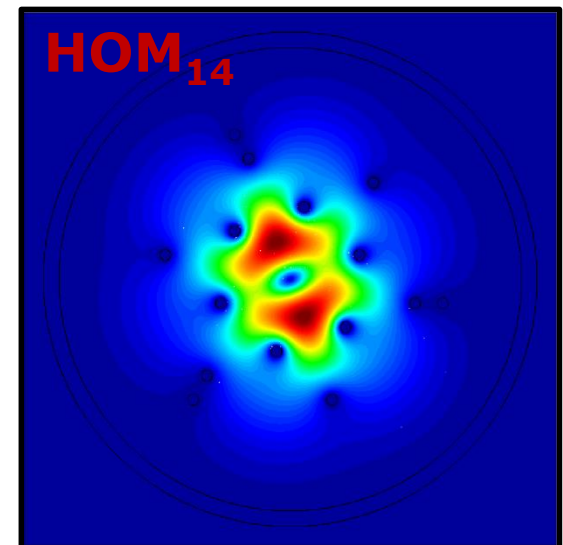
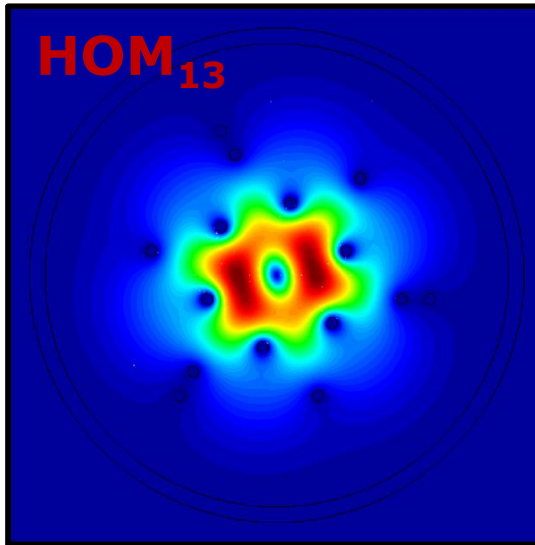
FM and HOM magnetic  
field modulus  
distributions at the SM  
range edge, for  
 $q \approx 41 \text{ W/m}$



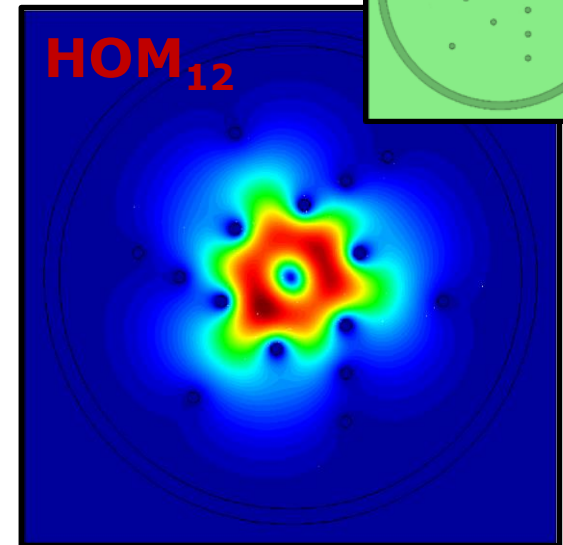
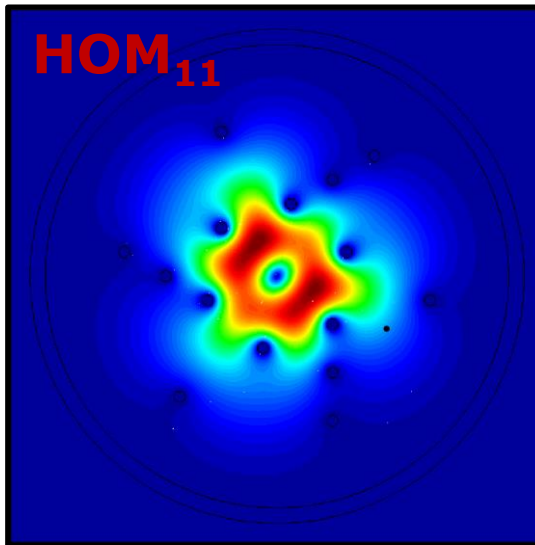
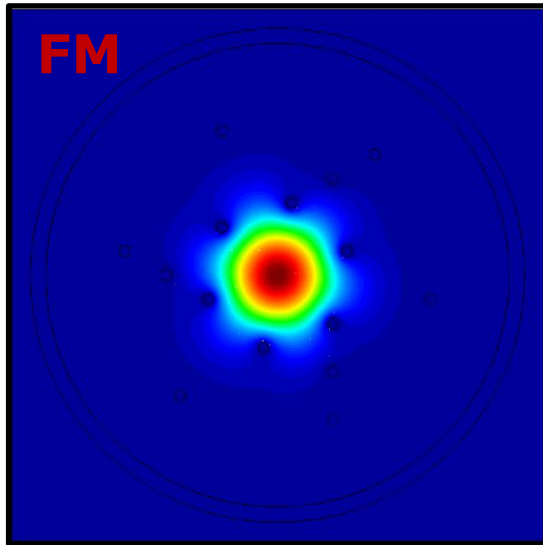
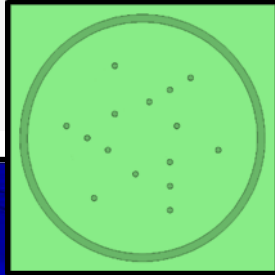
# Fiber b



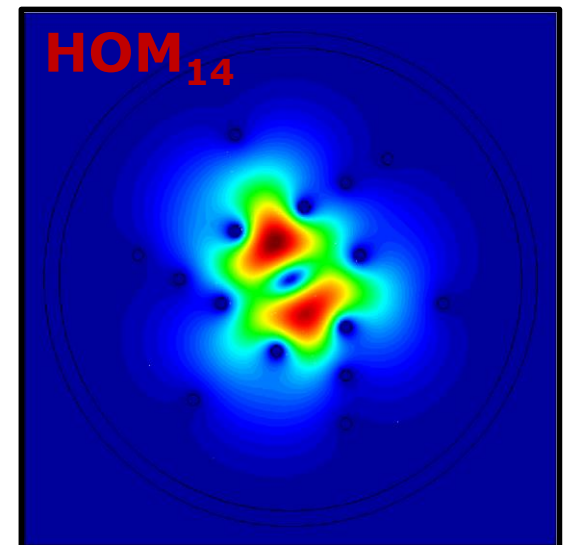
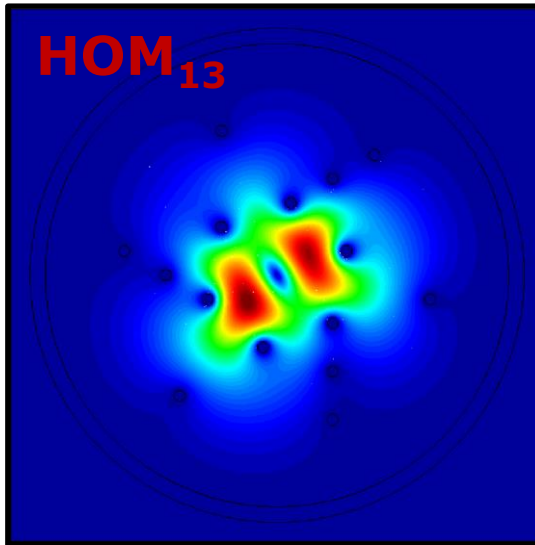
FM and HOM magnetic  
field modulus  
distributions at the SM  
range edge, for  
 $q \approx 47 \text{ W/m}$

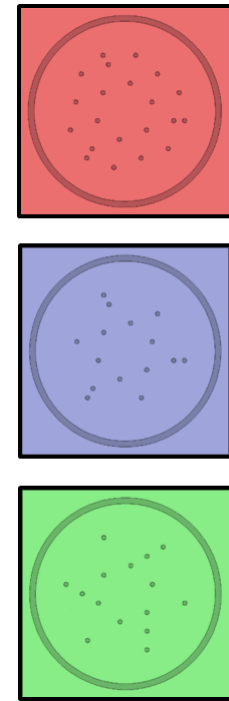
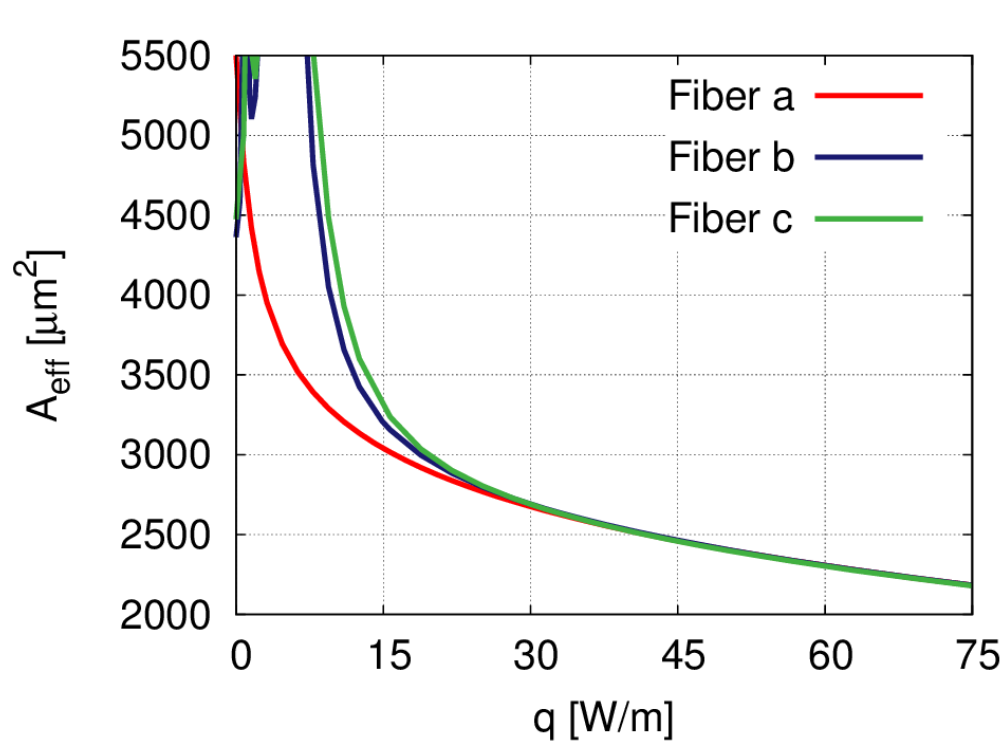


# Fiber c



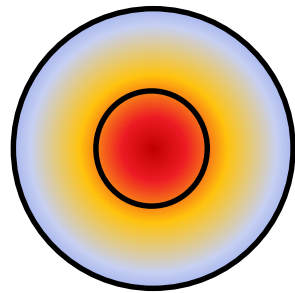
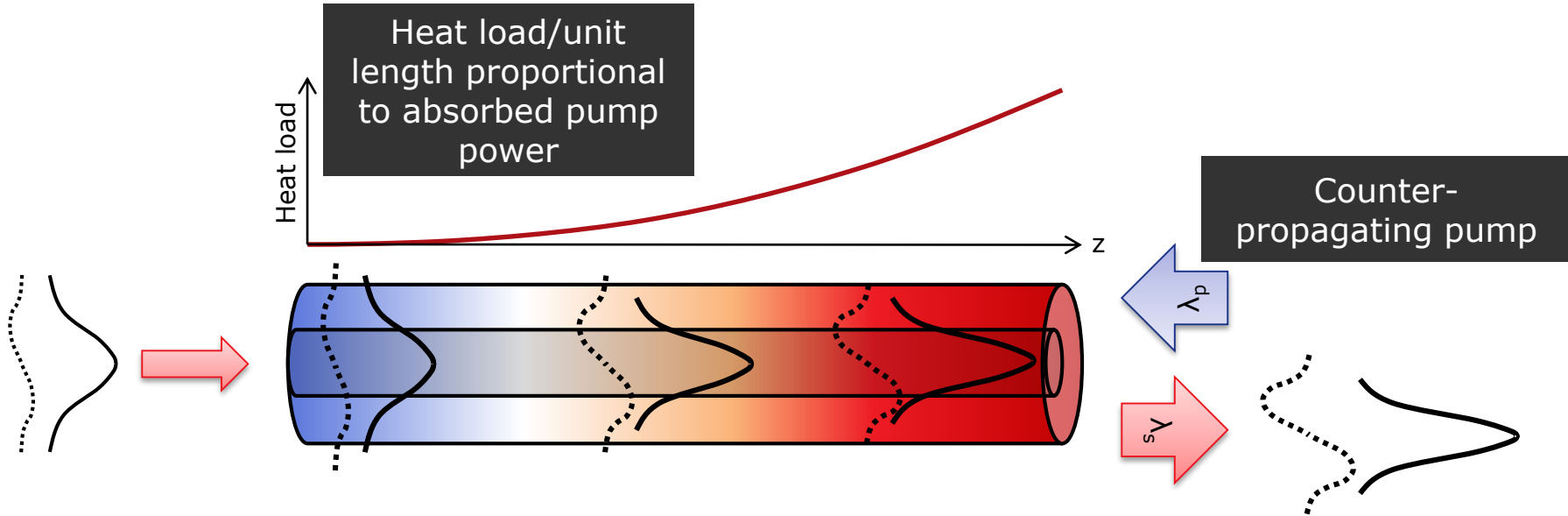
FM and HOM magnetic  
field modulus  
distributions at the SM  
range edge, for  
 $q \approx 50 \text{ W/m}$





- $A_{\text{eff}}$  values of **Fiber c** very similar to the ones of **Fiber b** in all the  $q$  range where the FM is well confined ( $q \geq 7 \text{ W/m}$ ) due to the cross-section geometry similarity
- The three PCFs have the same effective area for  $q \geq 25 \text{ W/m}$  = FM guiding no longer influenced by inner cladding geometry, being provided mainly by the index gradient caused by thermal effects

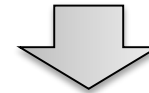
# Thermal effects along z



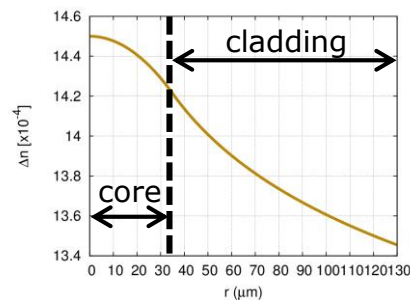
Higher temperature in the core  
Thermally-induced graded-index profile

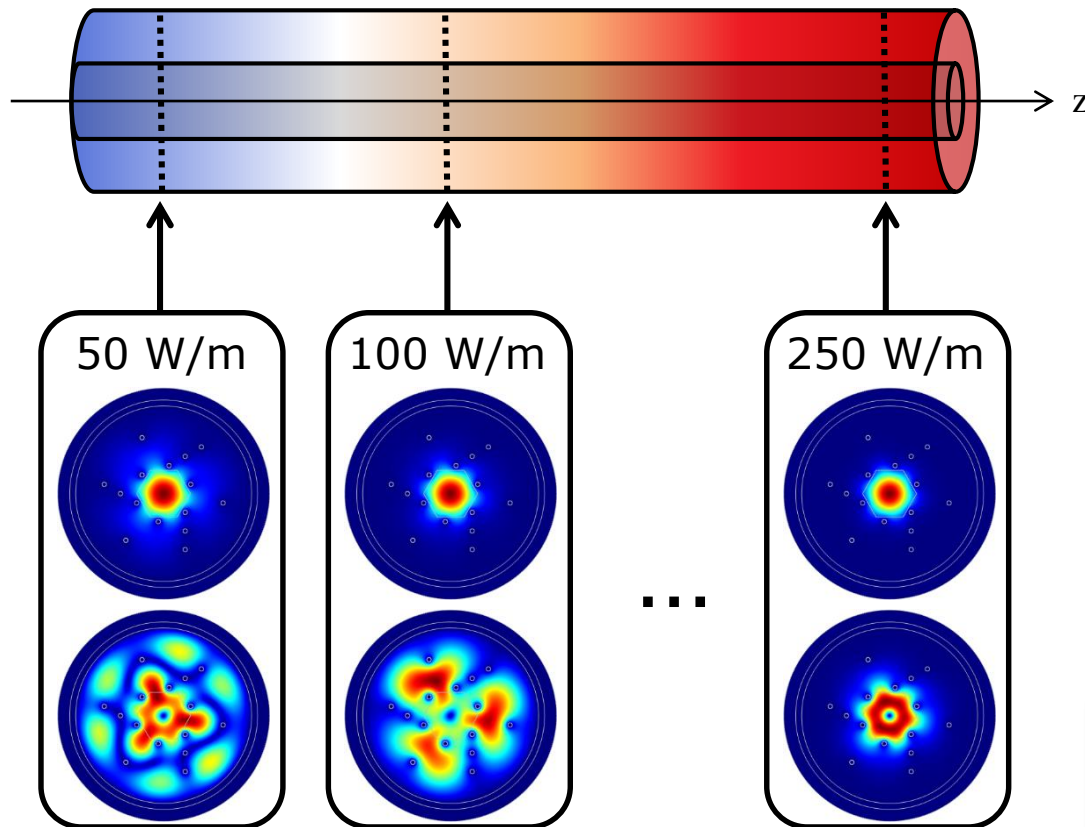


Increase confinement of high-order modes



Loss of transverse single mode output

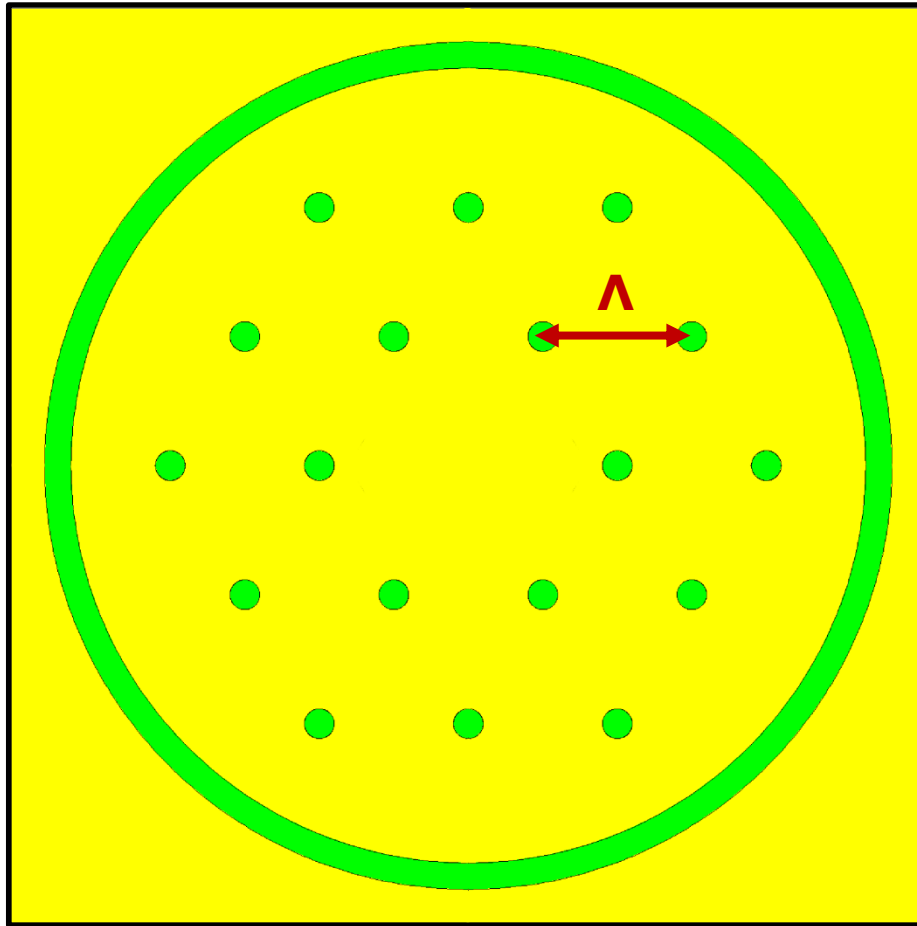




- At any step along  $z$ , use FEM solver to calculate field distribution of each guided mode
- Calculate amplifier gain, population inversion, generated heat, according to thermally-influenced field distribution
- Obtain heat load at  $z+\Delta z$  and calculate new field distribution
- Iterate back and forth

No approximations on fiber cross-section  
Possible to consider resonant effects

Fast computation



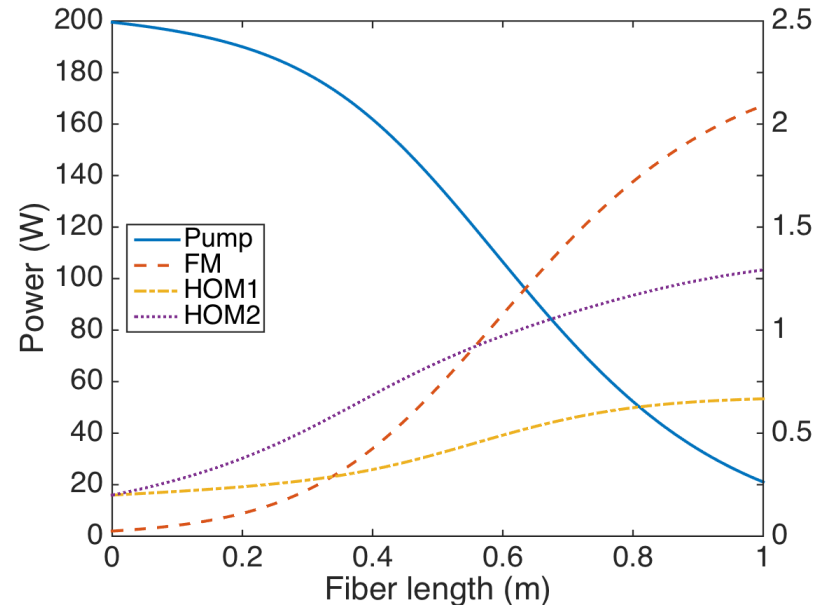
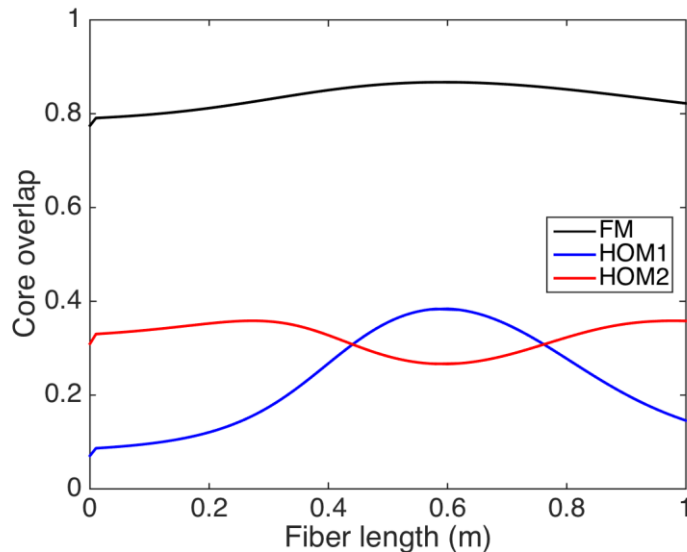
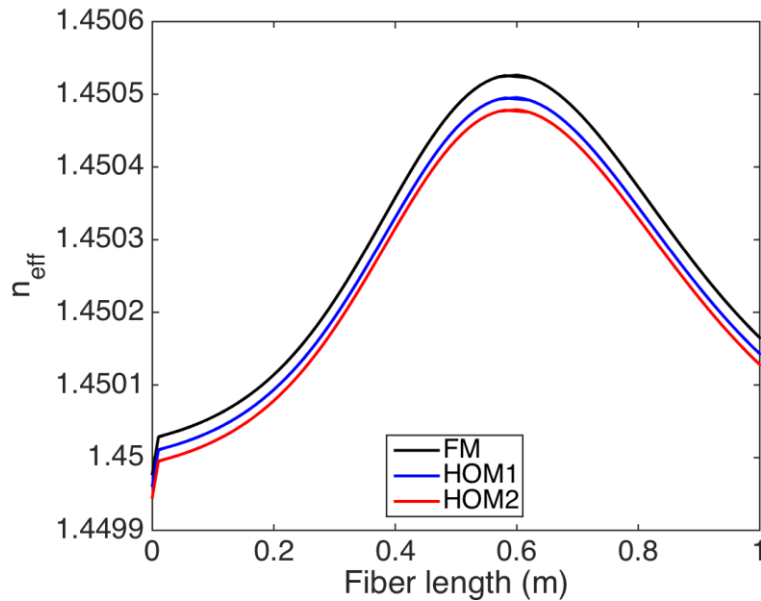
## LPF45

Hexagonal core area

Air-hole diameter:  $d = 9 \mu\text{m} = 0.2\Lambda$

Pitch:  $\Lambda = 45 \mu\text{m}$

# Gain competition in LPF45



LPF45, forward pump

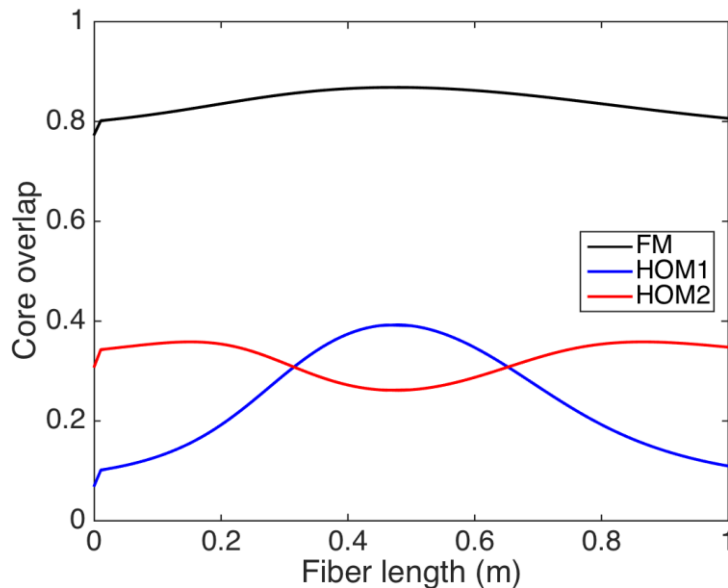
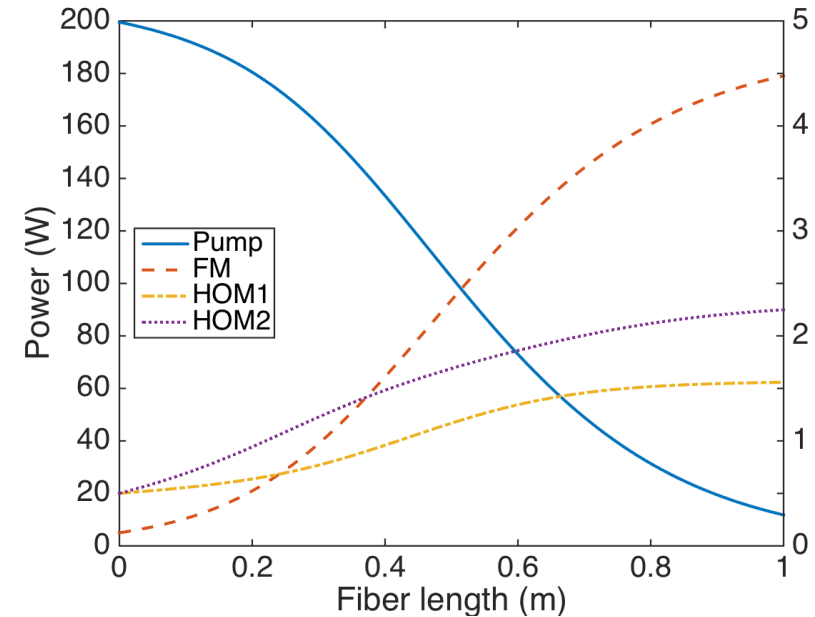
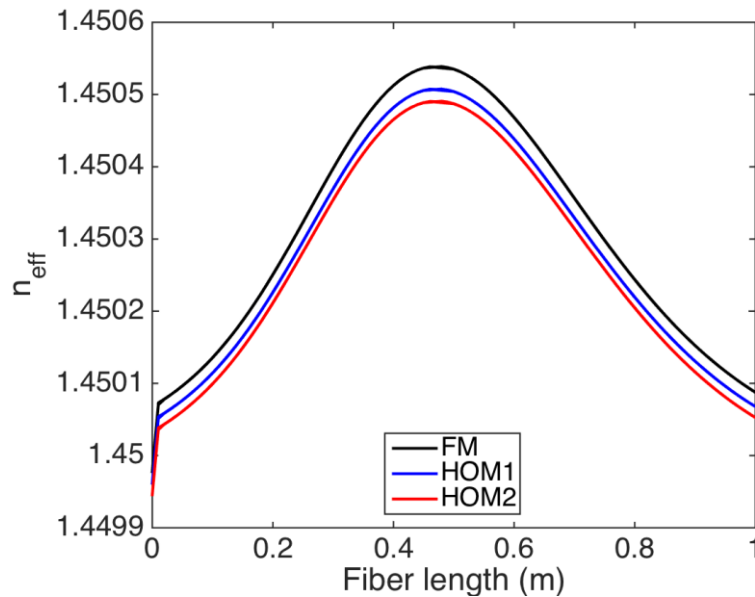
$$P_p^+ = 200 \text{ W}$$

$$P_{\text{FM}} = 2 \text{ W (G = 19.2 dB)}$$

$$P_{\text{HOM1}} = 200 \text{ mW (G = 5.2 dB)}$$

$$P_{\text{HOM2}} = 200 \text{ mW (G = 8.1 dB)}$$

# Gain competition in LPF45



LPF45, forward pump

$$P_p^+ = 200 \text{ W}$$

$$P_{\text{FM}} = 5 \text{ W (G = 15.5 dB)}$$

$$P_{\text{HOM1}} = 500 \text{ mW (G = 4.9 dB)}$$

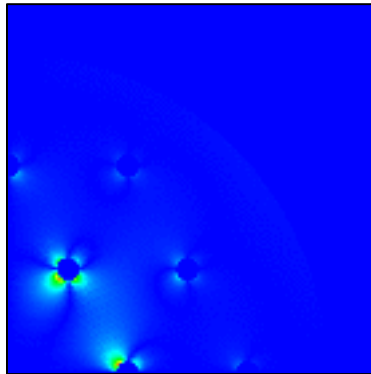
$$P_{\text{HOM2}} = 500 \text{ mW (G = 6.5 dB)}$$

# Gain competition in LPF45

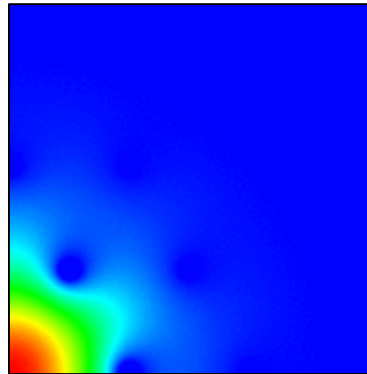
$$P_{\text{FM}} = 5 \text{ W}$$

Fundamental  
Mode

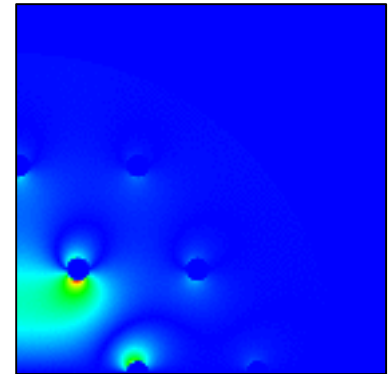
$H_x$



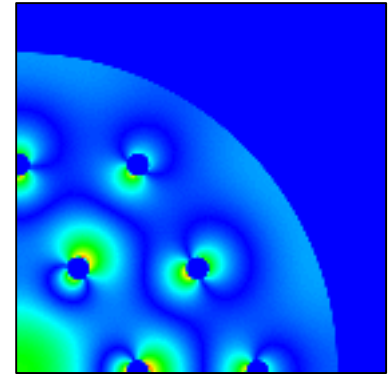
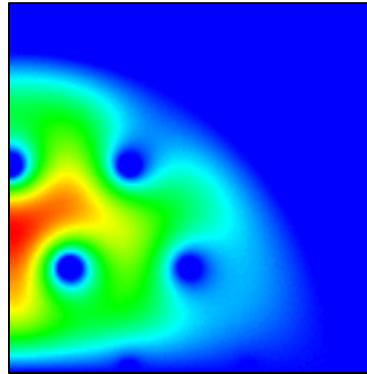
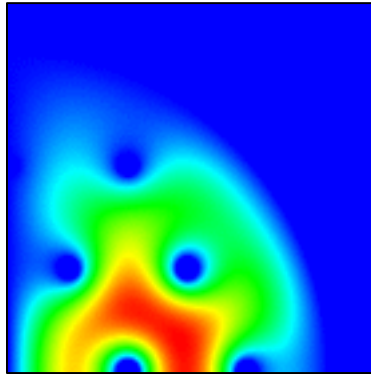
$H_y$



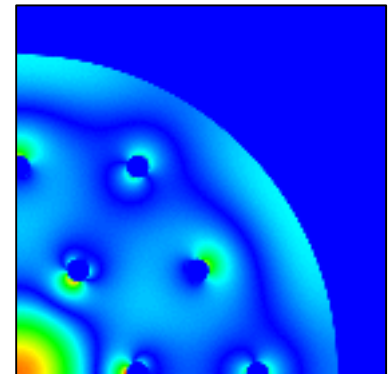
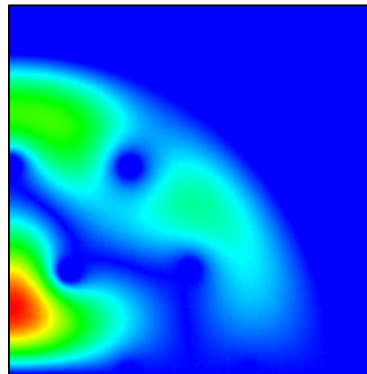
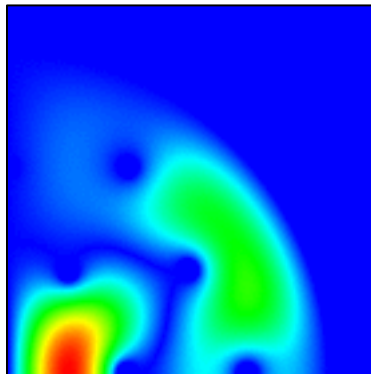
$H_z$



1<sup>st</sup> Higher-  
Order Mode



2<sup>nd</sup> Higher-  
Order Mode



- New LMA PCFs with reduced symmetry inner cladding design proposed
- Thermal effect influence on the SM properties and the effective area of the new fibers analyzed
- Good SM properties demonstrated for the reduced symmetry fibers at quite high pump power values
- NO FM guidance for low pump power values and in the absence of the pump in the asymmetric fibers with lower effective refractive index difference
- Significant effective area decrease in the SM range obtained for all the fibers with reduced symmetry inner cladding
- Similar SM properties obtained for asymmetric fibers with analogous effective refractive index distribution
- New model for pump and thermal load evolution along the fiber length, able to describe gain competition.

# Acknowledgments

<http://gaem.tlc.unipr.it/>



Stefano  
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Annamaria  
Cucinotta



Federica  
Poli



Michele  
Sozzi



Enrico  
Coscelli



Lorenzo  
Rosa



Carlo  
Molardi

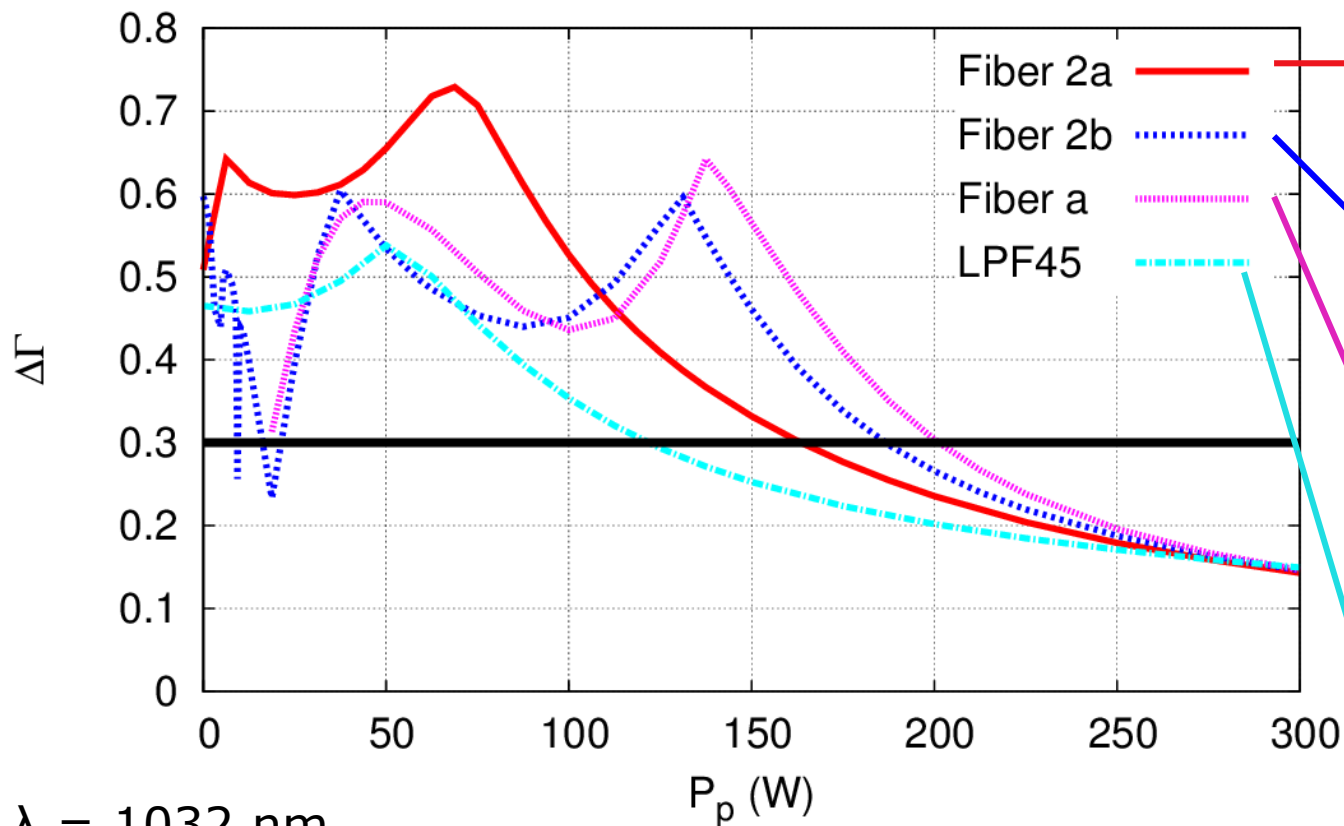


Alessandro  
Candiani



Thank you!

# Mode discrimination $\Delta\Gamma$



$\lambda = 1032$  nm

Differential overlap  $\Delta\Gamma$  (difference between FM and HOM)  
considered to define the Single Mode region:  $>0.3$

Non-symmetric design allows better HOM  
discrimination under higher heat load

