



# *Optical properties of rare-earth doped oxyfluoride glasses*

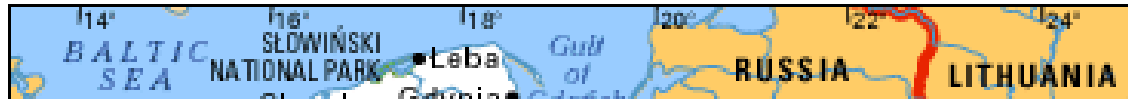
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## ***Outline***

- ***Introduction***
- ***Linear optical properties of rare-earth doped oxyfluoride glasses***
  - ***Absorption spectra***
  - ***Refractive index ( $n$ ) and extinction coefficient ( $k$ )***
  - ***Optical energy band gap***
- ***Nonlinear optical properties of rare-earth doped oxyfluoride glasses***
  - ***Third order nonlinear optical susceptibility***
    - ***Nonlinear transmission***
    - ***Degenerate Four Wave Mixing***
- ***Conclusions***



- ***$Er^{3+}$  and  $Yb^{3+}$  -doped glasses***

- Rare-earth doped optical waveguides are well known for
  - their amplifying and lasing characteristics

but may also be of interest for

- their intensity-dependent refractive index ( $n_2$ ).

- Precise knowledge of the dispersion of **absorption coefficient**, **linear** and **nonlinear refractive index** of the rare-earth doped oxyfluoride glasses is especially important for:
  - opto-electronic device applications,
  - all-optical switching device,
  - integrated-optics working over a wide wavelength range.



■ **Materials**

✓ Studied composition:

32(SiO<sub>2</sub>):9(AlO<sub>1.5</sub>):31.5(CdF<sub>2</sub>):18.5(PbF<sub>2</sub>):5.5(ZnF<sub>2</sub>):3.5(**RE**-F<sub>3</sub>) mol%,  
where RE: **Er**<sup>3+</sup> or **Yb**<sup>3+</sup>

1 <b>H</b>																	2 <b>He</b>	
3 <b>Li</b>	4 <b>Be</b>																	10 <b>Ne</b>
11 <b>Na</b>	12 <b>Mg</b>																	18 <b>Ar</b>
19 <b>K</b>	20 <b>Ca</b>	21 <b>Sc</b>	22 <b>Ti</b>	23 <b>V</b>	24 <b>Cr</b>	25 <b>Mn</b>	26 <b>Fe</b>	27 <b>Co</b>	28 <b>Ni</b>	29 <b>Cu</b>	30 <b>Zn</b>	31 <b>Ga</b>	32 <b>Ge</b>	33 <b>As</b>	34 <b>Se</b>	35 <b>Br</b>	36 <b>Kr</b>	
37 <b>Rb</b>	38 <b>Sr</b>	39 <b>Y</b>	40 <b>Zr</b>	41 <b>Nb</b>	42 <b>Mo</b>	43 <b>Tc</b>	44 <b>Ru</b>	45 <b>Rh</b>	46 <b>Pd</b>	47 <b>Ag</b>	48 <b>Cd</b>	49 <b>In</b>	50 <b>Sn</b>	51 <b>Sb</b>	52 <b>Te</b>	53 <b>I</b>	54 <b>Xe</b>	
55 <b>Cs</b>	56 <b>Ba</b>	57 <b>La</b>	72 <b>Hf</b>	73 <b>Ta</b>	74 <b>W</b>	75 <b>Re</b>	76 <b>Os</b>	77 <b>Ir</b>	78 <b>Pt</b>	79 <b>Au</b>	80 <b>Hg</b>	81 <b>Tl</b>	82 <b>Pb</b>	83 <b>Bi</b>	84 <b>Po</b>	85 <b>At</b>	86 <b>Rn</b>	
87 <b>Fr</b>	88 <b>Ra</b>	89 <b>Ac</b>	104 <b>Rf</b>	105 <b>Ha</b>	106 <b>Sg</b>	107 <b>Ns</b>	108 <b>Hs</b>	109 <b>Mt</b>	110 <b>Uun</b>									

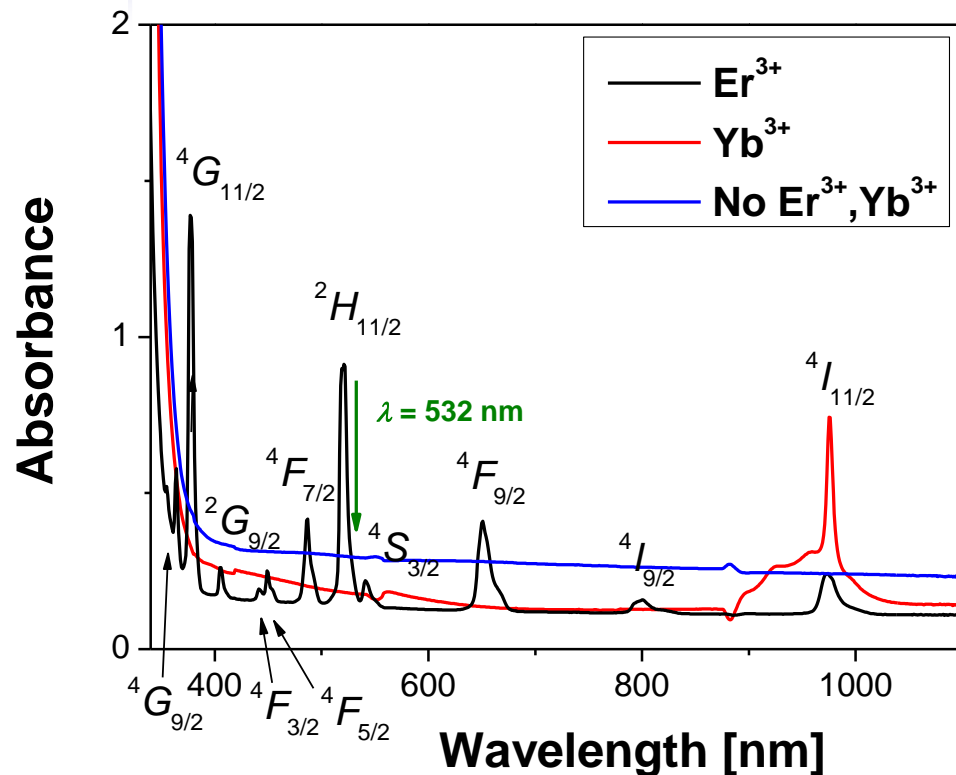
- Er<sup>3+</sup>-doped oxyfluoride glass;
- Yb<sup>3+</sup>-doped oxyfluoride glass;
- non-doped oxyfluoride glass.

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58 <b>Ce</b>	59 <b>Pr</b>	60 <b>Nd</b>	61 <b>Pm</b>	62 <b>Sm</b>	63 <b>Eu</b>	64 <b>Gd</b>	65 <b>Tb</b>	66 <b>Dy</b>	67 <b>Ho</b>	68 <b>Er</b>	69 <b>Tm</b>	70 <b>Yb</b>	71 <b>Lu</b>
90 <b>Th</b>	91 <b>Pa</b>	92 <b>U</b>	93 <b>Np</b>	94 <b>Pu</b>	95 <b>Am</b>	96 <b>Cm</b>	97 <b>Bk</b>	98 <b>Cf</b>	99 <b>Es</b>	100 <b>Fm</b>	101 <b>Md</b>	102 <b>No</b>	103 <b>Lr</b>

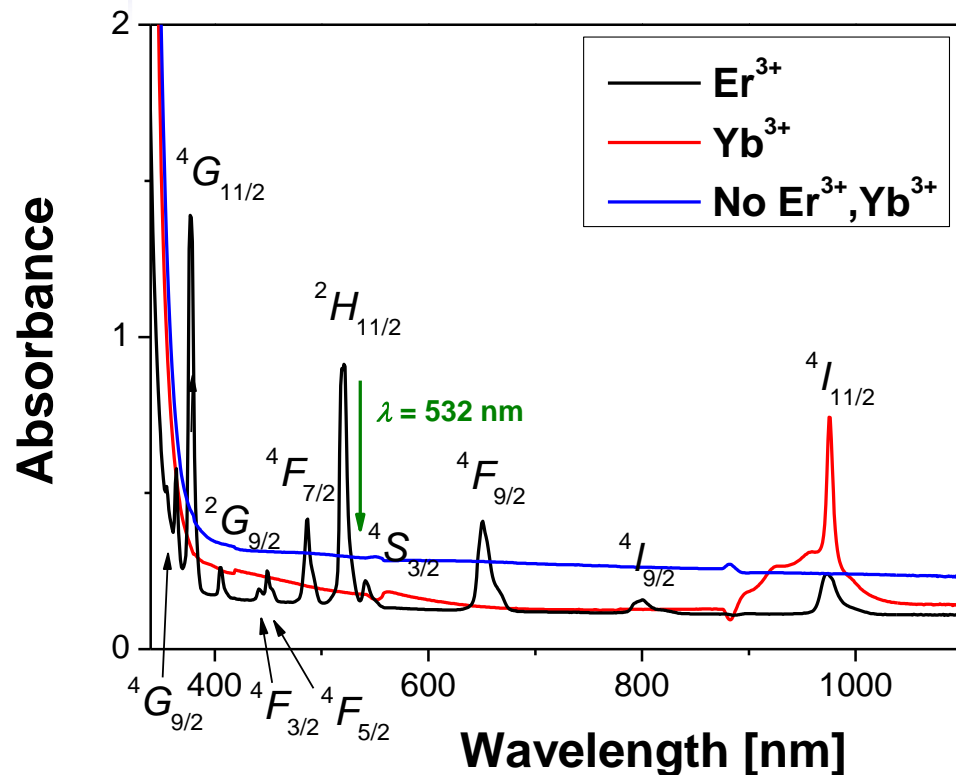


## ■ Absorption spectra of $\text{Er}^{3+}$ and $\text{Yb}^{3+}$



- ✓ linear absorption spectra of  $\text{Er}^{3+}$ -doped glass displayed 11 absorption bands corresponding to  $\text{Er}^{3+}$  transitions from ground state,  $^4I_{15/2}$ , to various excited states;
- ✓ the absorption bands,  $^4I_{15/2} \rightarrow ^4G_{11/2}$  and  $^4I_{15/2} \rightarrow ^2H_{11/2}$  located at 377 and 521 nm, are most intense and are called hypersensitive transitions (HSTs);
- ✓ HSTs are sensitive to small changes of environment around rare-earth ions.

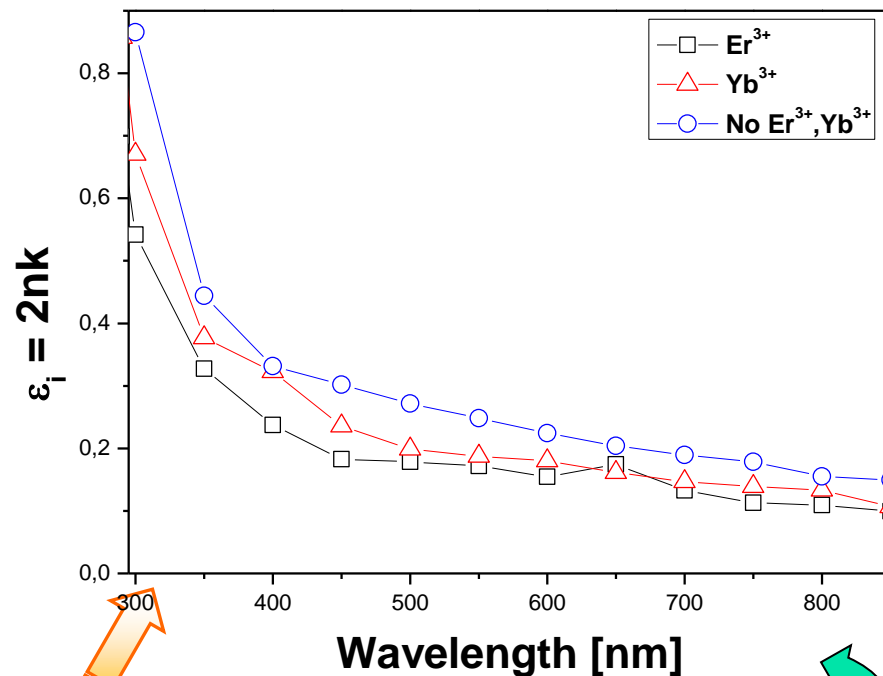
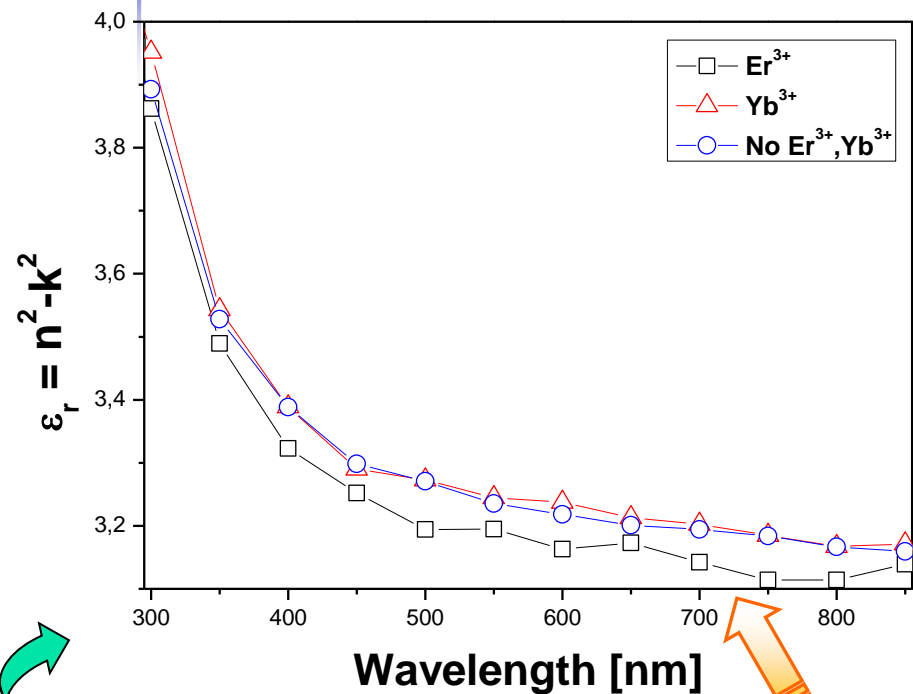
## ■ Absorption spectra of $\text{Er}^{3+}$ and $\text{Yb}^{3+}$



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✓ in the case of  $\text{Yb}^{3+}$ -doped glass there are one big band at 975nm and small at 560 nm.

## Real ( $\epsilon_r$ ) and imaginary ( $\epsilon_i$ ) parts of the dielectric constant



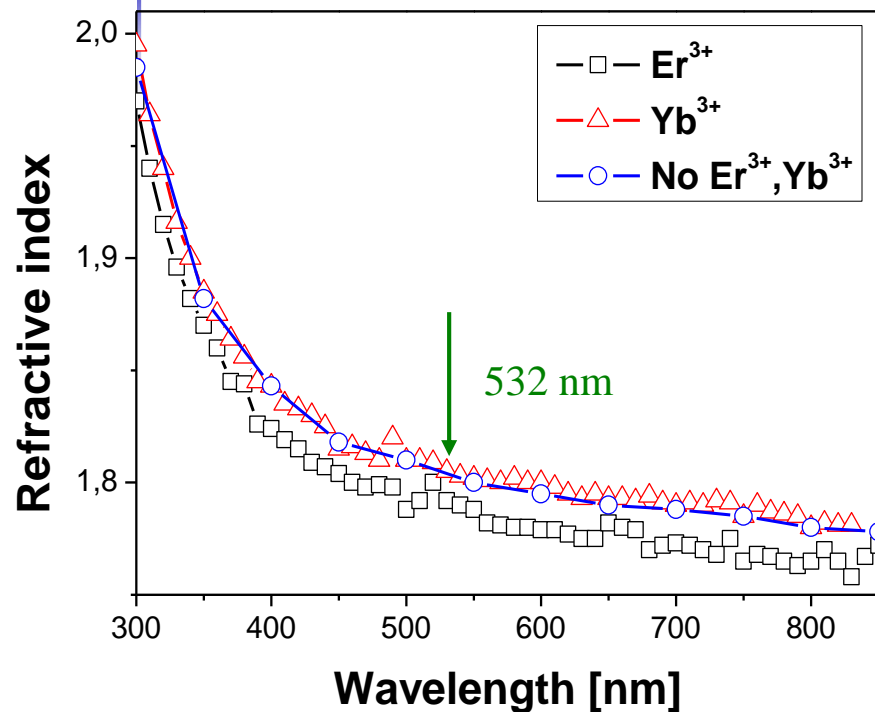
Real part ( $\epsilon_r$ )  
is associated with the term  
that shows how much  
it will lower the speed of light  
in the material

$$\begin{cases} \epsilon_r = n^2 - k^2 \\ \epsilon_i = 2nk \end{cases}$$

Imaginary part ( $\epsilon_i$ ) shows  
how a material absorbs  
energy from an electric field



## ■ Refractive index of $\text{Er}^{3+}$ and $\text{Yb}^{3+}$

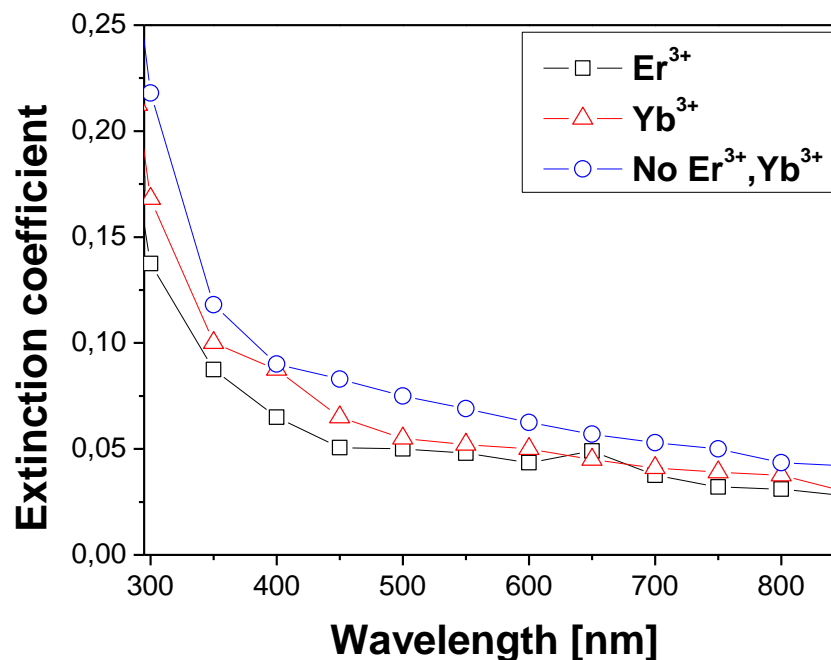


Samples	$n_{532\text{nm}}$
$\text{Er}^{3+}$	1.79
$\text{Yb}^{3+}$	1.81
No	1.81

- ✓ far from the absorption bands and beyond the optical band gap,  $n \searrow$  with  $\nearrow \lambda$  thus displaying normal dispersion;
- ✓ this behaviour can be described using a well-known first order Sellmeier relation.



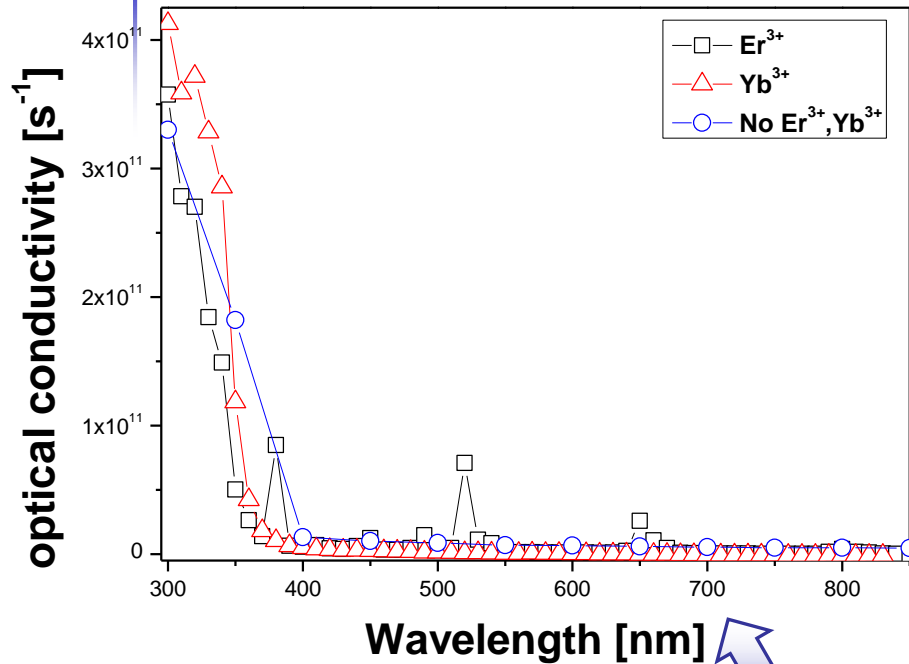
## ■ *Extinction coefficient*



- ✓  $k$  is a measure of the fraction of light lost due to reflection, scattering and absorption per unit distance of the participating medium;
- ✓  $k \searrow$  with  $\nearrow \lambda \Rightarrow$  the fraction of light lost due to reflection, scattering and absorbance decreases.



## Optical conductivity



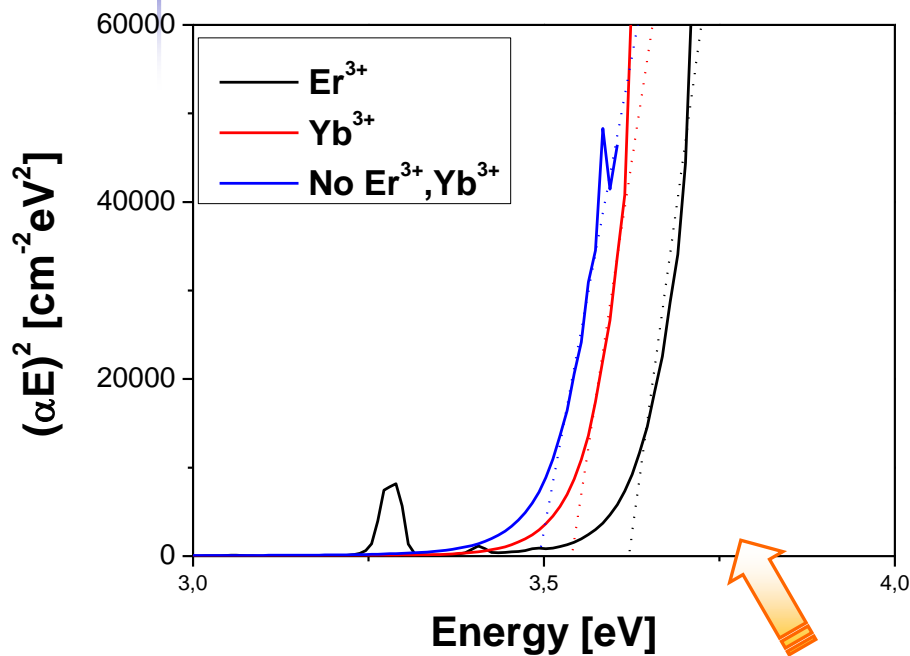
Samples	$n$	$\alpha$ $\text{cm}^{-1}$	$\sigma$ $\text{s}^{-1}$
$\text{Er}^{3+}$	1.79	3.12	$1.33 \cdot 10^{10}$
$\text{Yb}^{3+}$	1.81	2.45	$1.06 \cdot 10^{10}$
No	1.81	2.68	$1.16 \cdot 10^{10}$

$$\sigma = \frac{\alpha n c}{4\pi}$$

$\lambda = 532 \text{ nm} = 2.33 \text{ eV}$

The optical response of the material is most conveniently studied in terms of the optical conductivity.

## Optical energy band gap of $\text{Er}^{3+}$ and $\text{Yb}^{3+}$



Samples	$E_g$ [eV]
$\text{Er}^{3+}$	3.65
$\text{Yb}^{3+}$	3.55
No	3.50

$$(\alpha h\nu) = B(h\nu - E_g^{\text{opt}})^n$$



Tauc method

where

$B$  is the band tailing parameter,

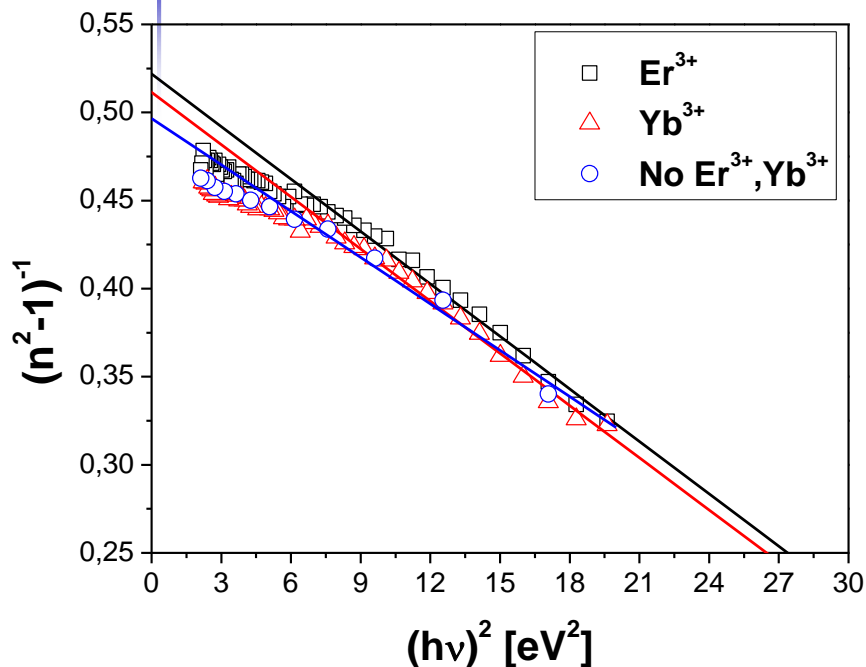
$n = 1/2$  for a direct allowed transition,

$n = 2$  for an indirect allowed transition,

$n = 3/2$  for a direct forbidden transition,

$n = 3$  for an indirect forbidden transition.

## Optical energy band gap



The values of  $E_0$  and  $E_d$  can be directly determined from the slope  $(E_0 E_d)^{-1}$  and the intercept on the vertical axis ( $E_0 / E_d$ ).

$$E_g = E_0 / 2$$

single-effective oscillator model -  
**Wemple and DiDomenico**

$$n^2 - 1 = \frac{E_d E_0}{E_0^2 - (h\nu)^2}$$

$E_0$  is the single oscillator energy  
(the average energy gap),

$E_d$  is the dispersion energy,  
which is a measure of the average strength  
of the interband optical transitions.

Samples	$E_0$ eV	$E_d$ eV	$E_g$ (W-D) eV
$\text{Er}^{3+}$	7.25	13.89	3.63
$\text{Yb}^{3+}$	7.19	14.07	3.60
No	7.05	16.49	3.53



■ *Optical energy band gap*

Samples	$E_g$ (W-D) [eV]	$E_g$ (T) [eV]
<b>Er<sup>3+</sup></b>	<b>3.63</b>	<b>3.65</b>
<b>Yb<sup>3+</sup></b>	<b>3.60</b>	<b>3.55</b>
<b>No</b>	<b>3.53</b>	<b>3.50</b>



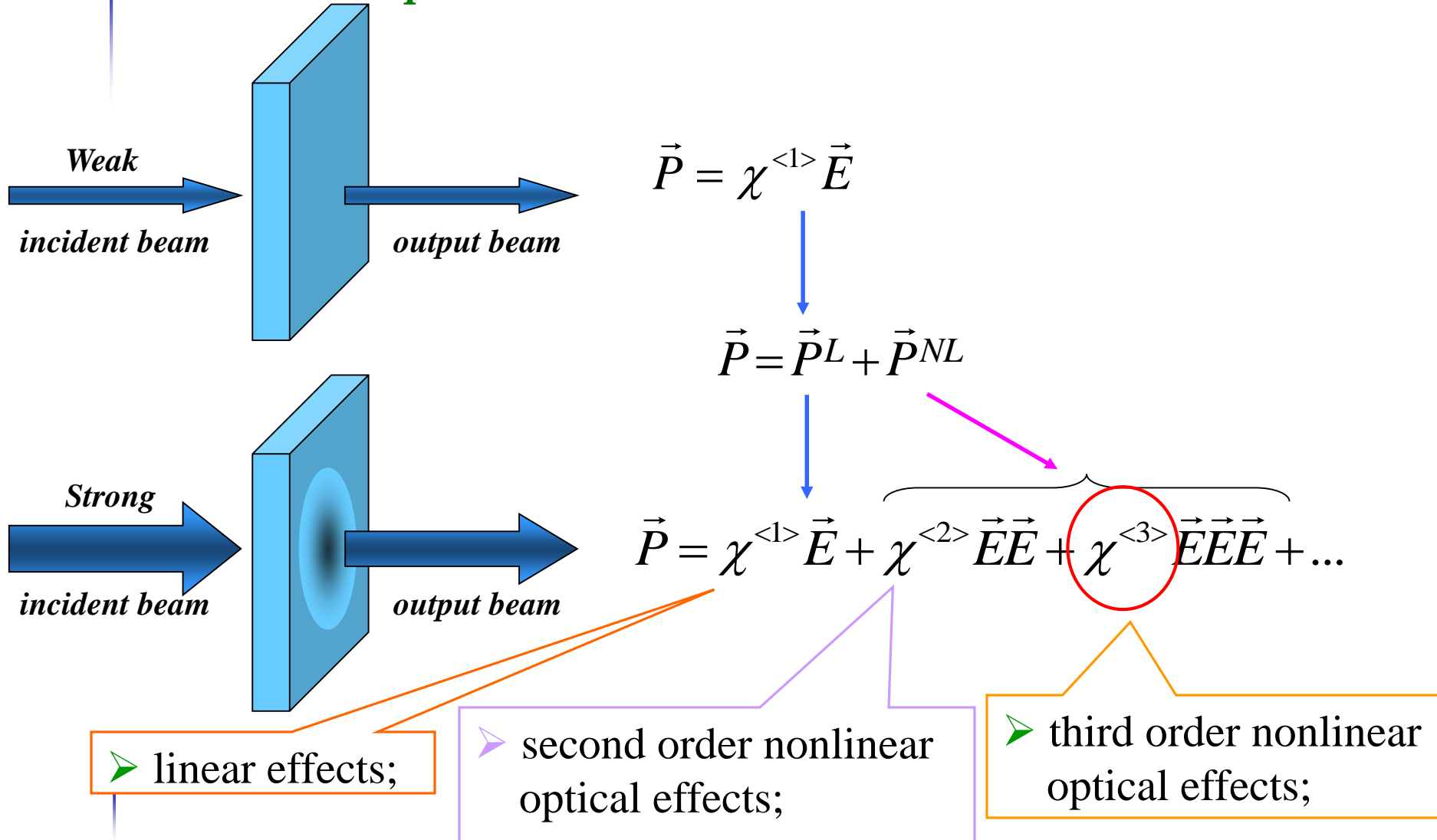
**Wemple and DiDomenico  
method**



**Tauc method**



## ■ *Nonlinear polarization*





- *Third order nonlinear optical susceptibility*

$$\chi^{<3>} = \chi_R^{<3>} + i\chi_I^{<3>}$$

related to the two photon absorption;

related to  
the nonlinear refractive index changes;

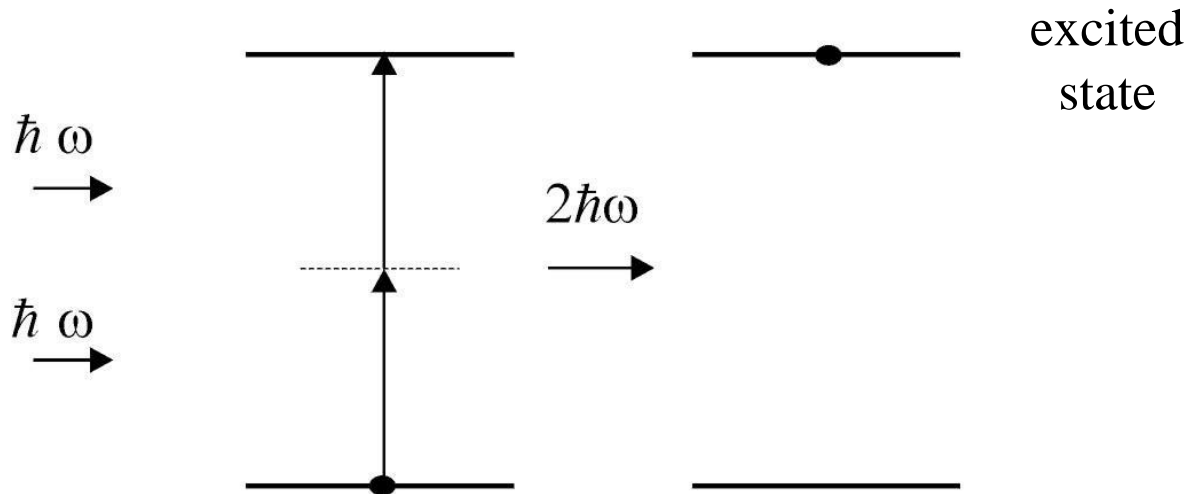
$$\chi_R^{<3>} = \frac{n^2 c}{12\pi^2} n_2$$

$$\chi_I^{<3>} = \frac{n^2 c \lambda}{48\pi^3} \beta$$

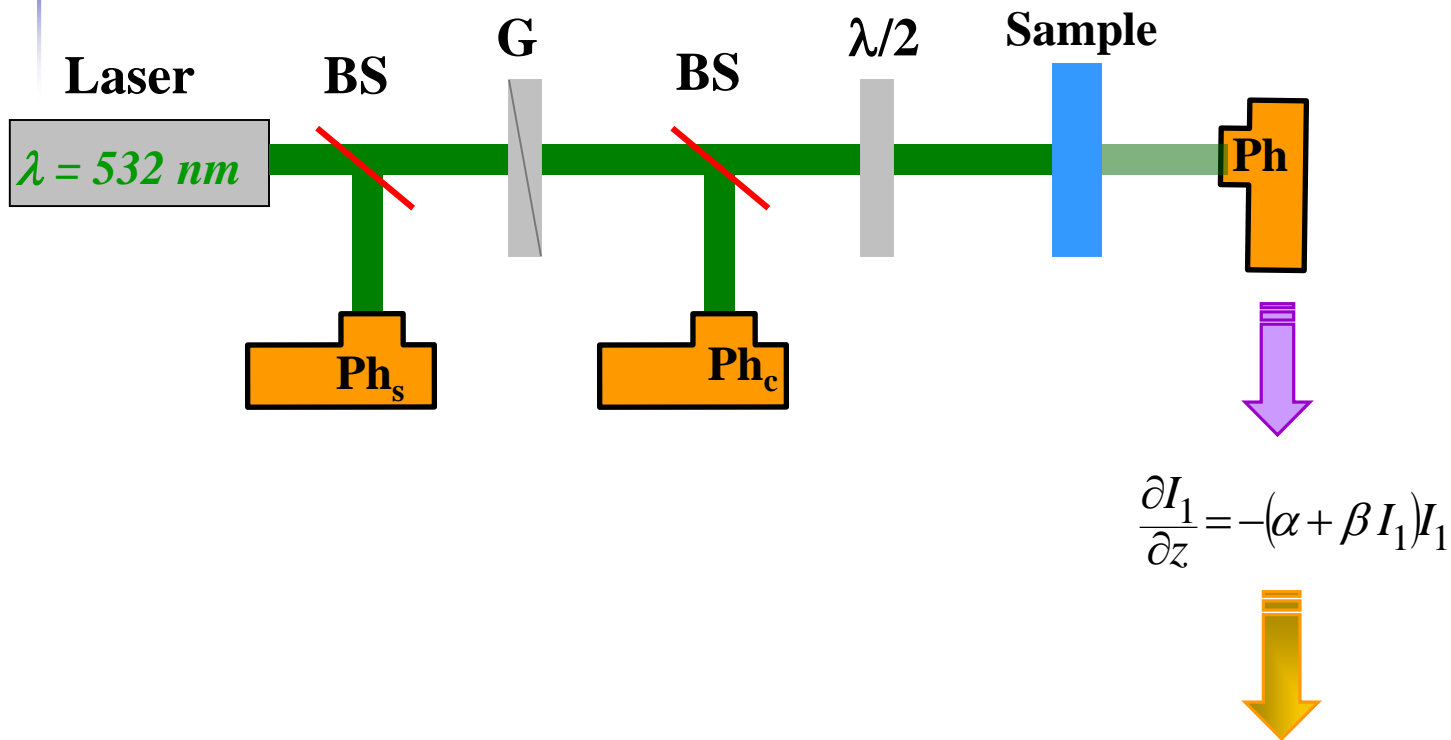


Two-photon absorption is the simultaneous absorption of two photons in order to excite the electron from a ground state to an excited state.

$$E_g / 2 < h\nu < E_g$$



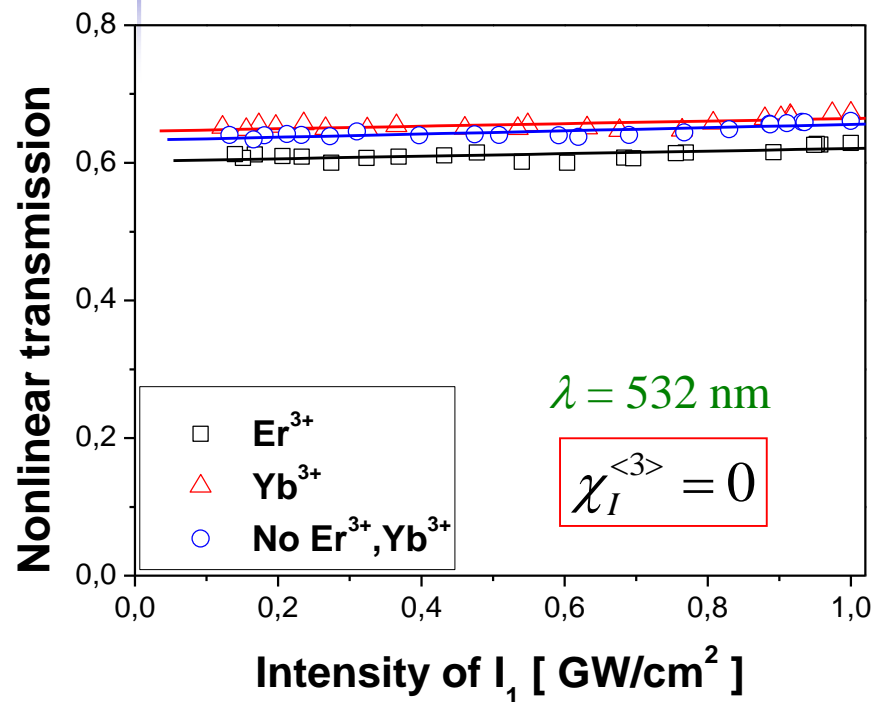
■ *Two Photon Absorption (nonlinear transmission)*



$$\beta = \frac{48\pi^3}{n^2 c \lambda} \chi_I^{(3)}$$

$$T = \frac{I(L)}{I(0)} = \frac{\alpha(1-R)^2 \exp(-\alpha L)}{\alpha + \beta I(0)(1-R)(1 - \exp(-\alpha L))}$$

# ■ *Nonlinear transmission of Er<sup>3+</sup> and Yb<sup>3+</sup>*



Samples	$\alpha$ [cm <sup>-1</sup> ]
Er <sup>3+</sup>	3.12
Yb <sup>3+</sup>	2.45
No	2.68

$$R = \frac{(n-1)^2}{(n+1)^2}$$

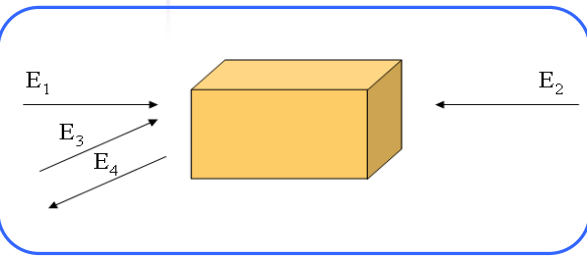
$$T = \frac{I(L)}{I(0)} = (1-R)^2 \exp(-\alpha L)$$

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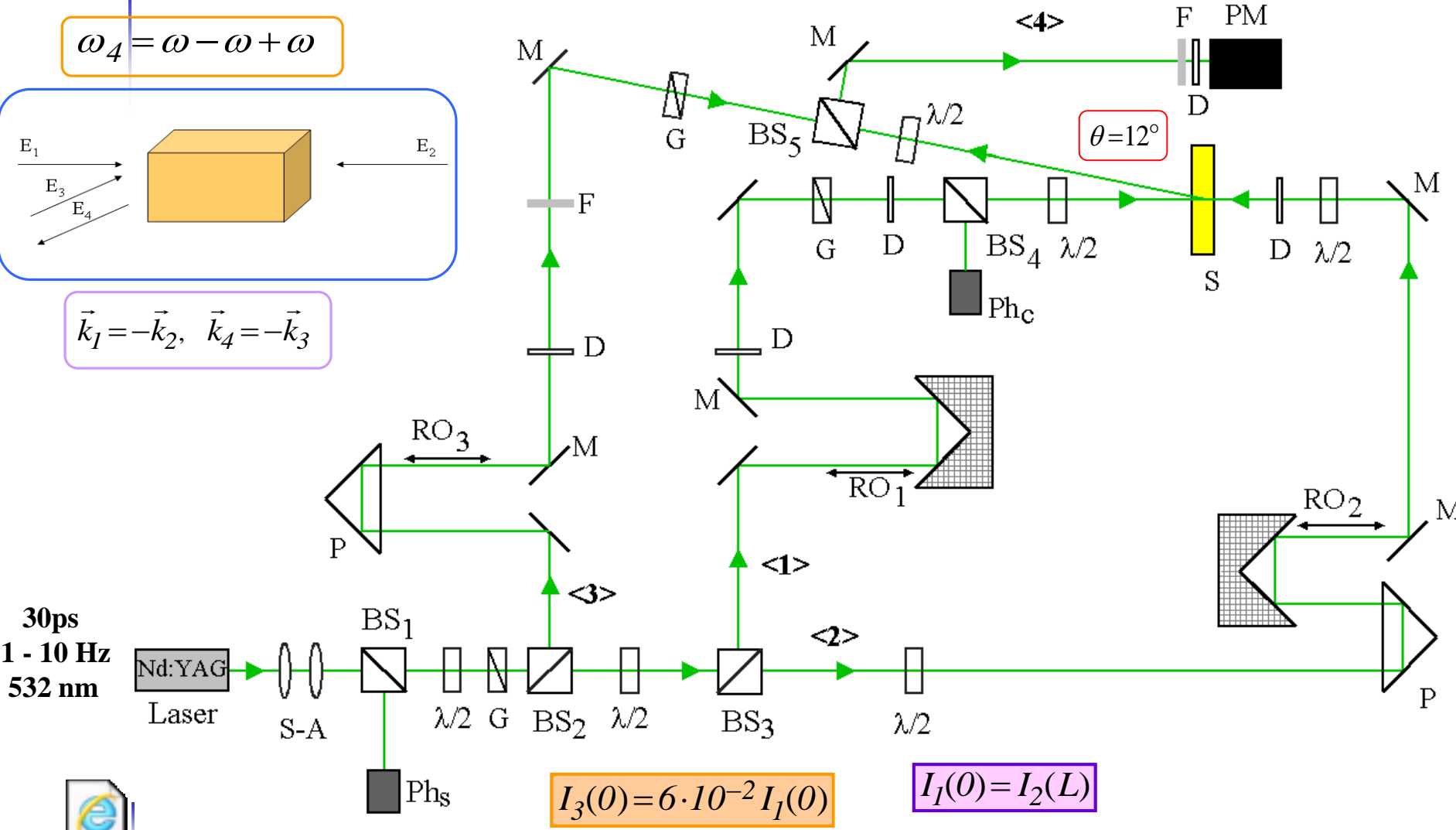
~~$$\chi_I^{<3>} = \frac{n^2 c \lambda}{48 \pi^3} \beta$$~~

# Degenerate Four Wave Mixing method

$$\omega_4 = \omega - \omega + \omega$$



$$\vec{k}_1 = -\vec{k}_2, \quad \vec{k}_4 = -\vec{k}_3$$



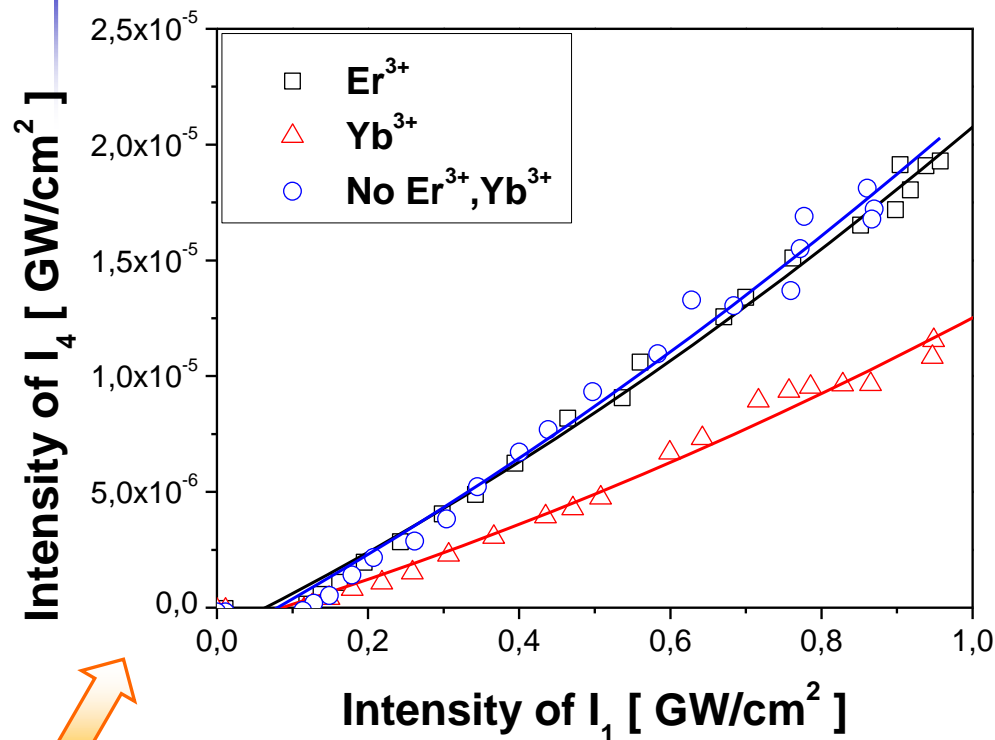
$$I_3(0) = 6 \cdot 10^{-2} I_1(0)$$

$$I_1(0) = I_2(L)$$





## ■ Degenerate Four Wave Mixing



Samples	$\chi^{<3>}$ [esu]
<b>Er<sup>3+</sup></b>	$2.78 \cdot 10^{-12}$
<b>Yb<sup>3+</sup></b>	$1.97 \cdot 10^{-12}$
<b>No</b>	$2.67 \cdot 10^{-12}$

$$R = \frac{I_4(0)}{I_3(0)} = \left( \frac{48\pi^3}{n^2 c \lambda} \chi^{<3>} \right)^2 \frac{I_1(0)I_2(0)\exp(-\alpha L)}{\left[ p \coth(pL) + \frac{\alpha}{2} \right]^2}$$

$$I_3(0) = 6 \cdot 10^{-2} I_1(0)$$

$$p^2 = \frac{\alpha^2}{4} - \left( \frac{48\pi^3}{n^2 c \lambda} \chi^{<3>} \right)^2 I_1(0)I_2(0)$$



■ *Third order nonlinear optical susceptibility  $\chi^{<3>}$*

$$\lambda = 532 \text{ nm} = 2.33 \text{ eV}$$

Samples	$L$ [mm]	$n$	$\alpha$ [cm <sup>-1</sup> ]	$\chi^{<3>} \cdot 10^{12}$ [esu]	$n_2 \cdot 10^{14}$ [cm <sup>2</sup> W <sup>-1</sup> ]	$F \cdot 10^{13}$ [esu cm]
Er <sup>3+</sup>	1.089	1.79	3.12	2.78	3.43	8.91
Yb <sup>3+</sup>	1.083	1.81	2.45	1.97	2.39	8.04
No	1.068	1.81	2.68	2.67	3.23	9.96

$$\chi_{SI}^{<3>} \left[ \frac{m^2}{V^2} \right] = 1.4 \cdot 10^{-8} \chi_{CGS}^{<3>} [esu]$$

$$n_2 = \frac{12\pi^2}{n^2 c} \chi^{<3>}$$

$$F = \frac{\chi^{<3>}}{\alpha}$$



## ■ *Conclusions*

- Linear and nonlinear optical properties of  $\text{Er}^{3+}$  and  $\text{Yb}^{3+}$  doped oxyfluoride glasses were determined;
- It was found that  $\chi^{(3)}$ ,  $\alpha$ ,  $\sigma$  and  $n_2$  of  $\text{Er}^{3+}$ -doped oxyfluoride glass are higher than for  $\text{Yb}^{3+}$ -doped oxyfluoride glass at 532 nm.
- It was found that  $E_g(\text{Er}^{3+}) > E_g(\text{Yb}^{3+}) > E_g(\text{No})$ .
- It should be also noted that the values of  $E_g$  calculated using the Wemple-DiDomenico method are in good agreement with those determined using the method of Tauc.

■ *Looking for collaboration*



Ellipsometer V-VASE (J.A.Woollam Co.) + FTIR device Sendira (Sentech GmbH):

- ✓ three angles of incidence:  $65^\circ$ ,  $70^\circ$  and  $75^\circ$ ,
- ✓ MIR–vis–UV spectral range: **193 nm** (6.5 eV) – **20 000 nm** (0.06 eV).

Luminescence measurements:

- ✓ UV-vis spectral range: 200 nm – 2000 nm,
- ✓ temperature range: 10 K - 300 K using 325 nm (He-Cd laser - 20 mW).

FTIR measurements:  $500\text{ cm}^{-1}$  –  $4000\text{ cm}^{-1}$ .

X-Ray Diffraction (XRD).

Atomic Force Microscopy (AFM).



■ *Looking for collaboration*

Thermal properties (such as diffusivities, effectivities and conductivities) using photopyroelectric and infrared radiometry techniques.

Raman Perkin-Elmer Raman-Micro 200 system:

✓ spectral range of 100 - 3200  $\text{cm}^{-1}$ .

The Raman scattering was excited using the near-infrared laser operating at 785 nm, collected in the backscattering geometry and detected using a CCD.

