

The Linewidth of MIR Intersubband Light Sources

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Theory of Semiconductor Materials and Optics

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Outline

- Origin of the α -factor
- Fundamental reason for nonzero ISB α
- The gain without inversion case
- Summary

Origin of the α factor

- Conventional laser – Schalow-Townes

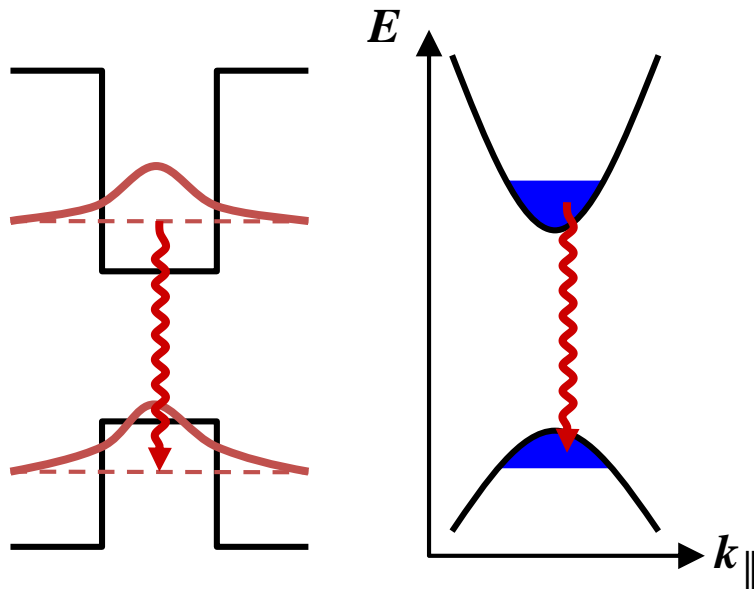
$$\Delta\nu_{ST} = A/n_{ss}$$

- A is the spontaneous emission coefficient and n_{ss} is the number of photons in the lasing mode at steady state.

- Semiconductor laser – Henry's α factor or linewidth enhancement factor

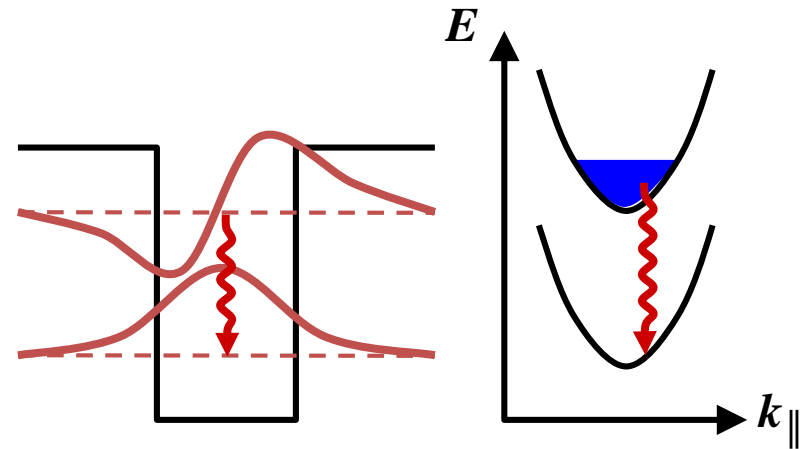
$$\Delta\nu = (1 + \alpha^2) \Delta\nu_{ST}$$

Interband vs. Intersubband Optics:



interband transition

- bipolar
- photon energy determined by bandgap energy E_{gap} of material



intersubband transition

- unipolar
- photon energy determined by well thickness, adjustable

The intersubband case

- In usual GaAg-AlGaAs the effective masses are almost the same on both upper and lower lasing subbands – leading to an almost exactly Lorentzian lineshape and *expected zero α factor at peak gain*.
- However, experimental results show values from -0.5 to 0.5 (subthreshold) and from 0.2 to 3 above threshold. (MIR). See L. Jumpertz et al AIP Advances 6, 015212 (2016).
- THz case: 0.2 to 0.5.

Origin of the nonzero α -factor

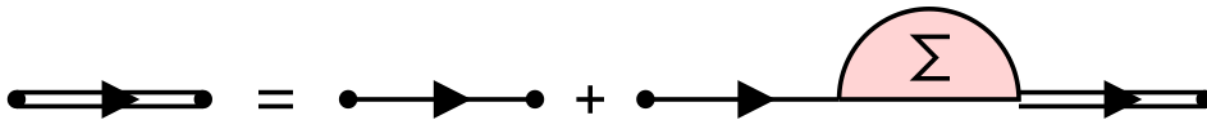
- A nonzero α at peak gain has been attributed to a combination of nonparabolicity and many-body effects. See Liu et al, *Optics Express* 21, 27804-27815 (2013).
- *However I show here that the most fundamental reason stems from considering counter-rotating terms in the optical susceptibility.*

Connection between Macroscopic Measurables and Microscopic Theory

$$\alpha(\omega) = -\frac{\delta\Re\{\chi(\omega)\}}{\delta\Im\{\chi(\omega)\}}$$

- The susceptibility is derived from the solutions of a NGFE approach.

$$\chi(\omega) = \sum_{i,j,k} \wp_{ij}(k) G_{ji}^<(\omega, k) / E(\omega) + \wp_{ji}(k) G_{ij}^<(\omega, k) / E(\omega)$$



Origin of the nonzero α -factor

- For parabolic bands and without manybody effects

$$\delta\chi(E) = \frac{\wp^2 \delta N}{V} \left[\frac{1}{E - \Delta + i\Gamma} - \frac{1}{E + \Delta + i\Gamma} \right]$$

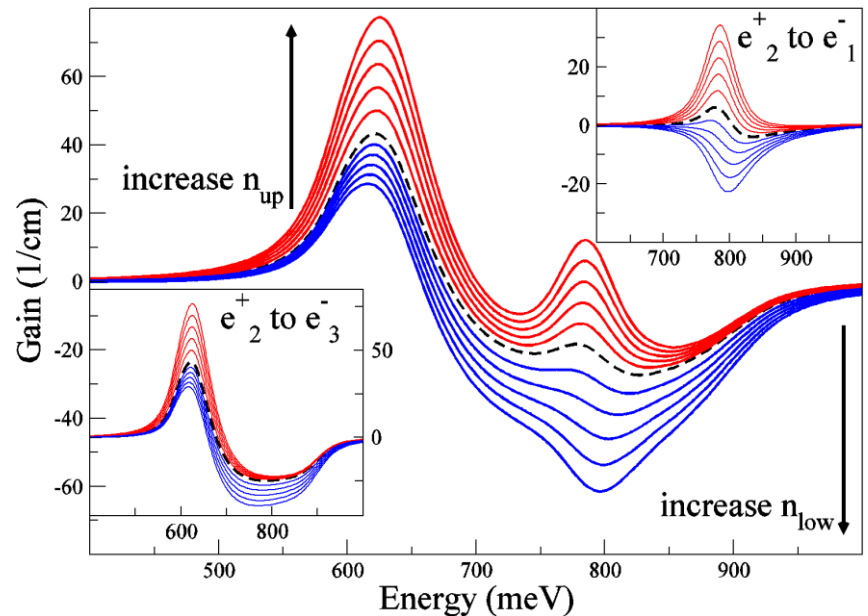
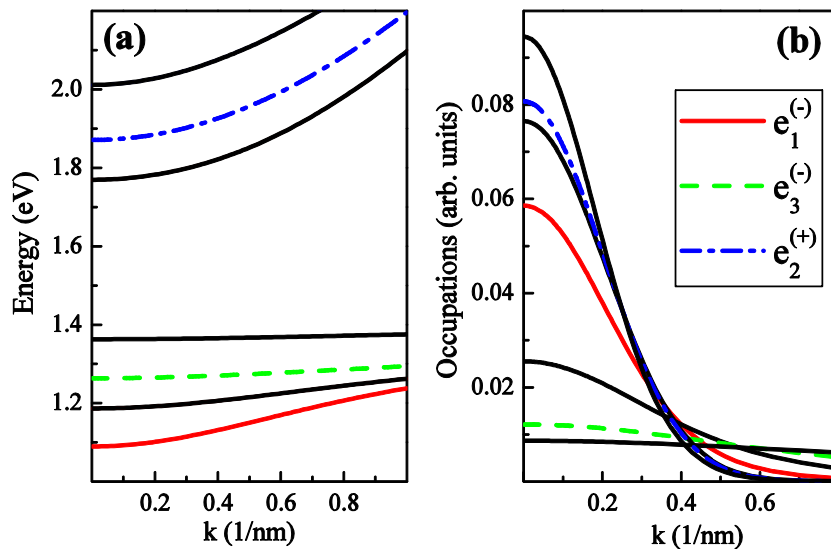
$$\alpha = \frac{\Delta^2 + \Gamma^2 - E^2}{2\Gamma E}$$

- The peak again is still almost exactly at the RWA resonance but the real part is nonzero due to the CRWA term. *However nonparabolicity and manybody effects are required to explain negative values.*

ISB Dilute Nitride Band Engineering

band structure and occupations -
local inversion - 7 nm
 $\text{Ga}_{0.98}\text{N}_{0.02}\text{As}/\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$

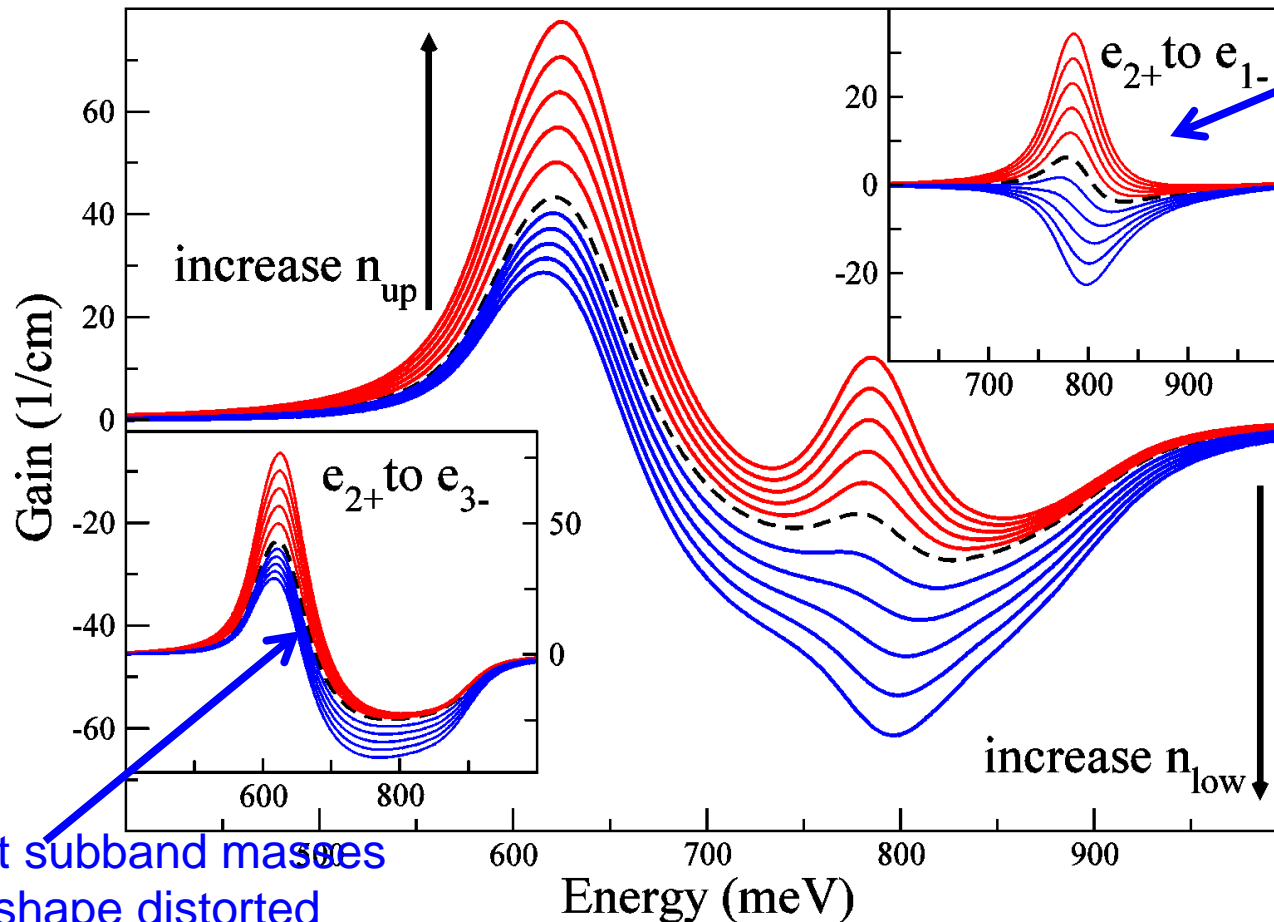
gain without inversion - dispersive
shape only for similar effective masses



M. F. Pereira and S. Tomić, Appl. Phys. Lett. 98, 061101 (2011).

ISB Gain without Global Inversion

similar subband masses -
dispersive shape

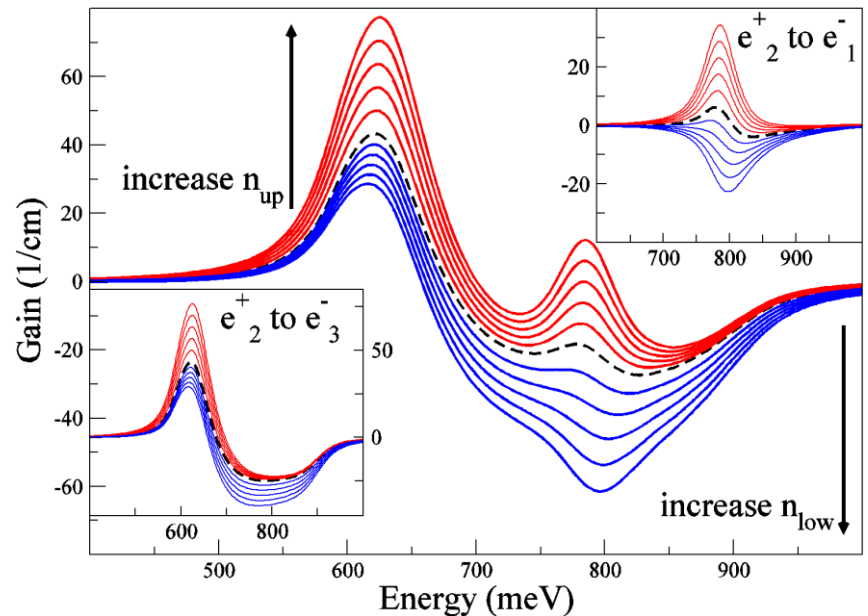
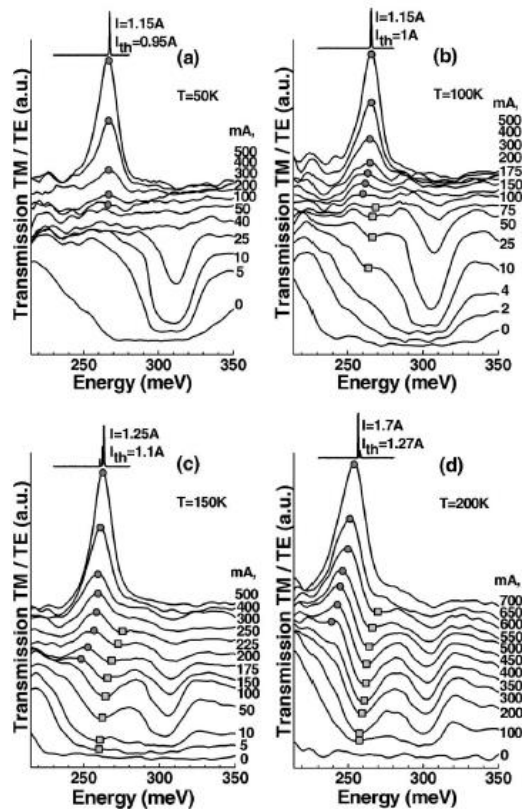


very different subband masses -
dispersive shape distorted

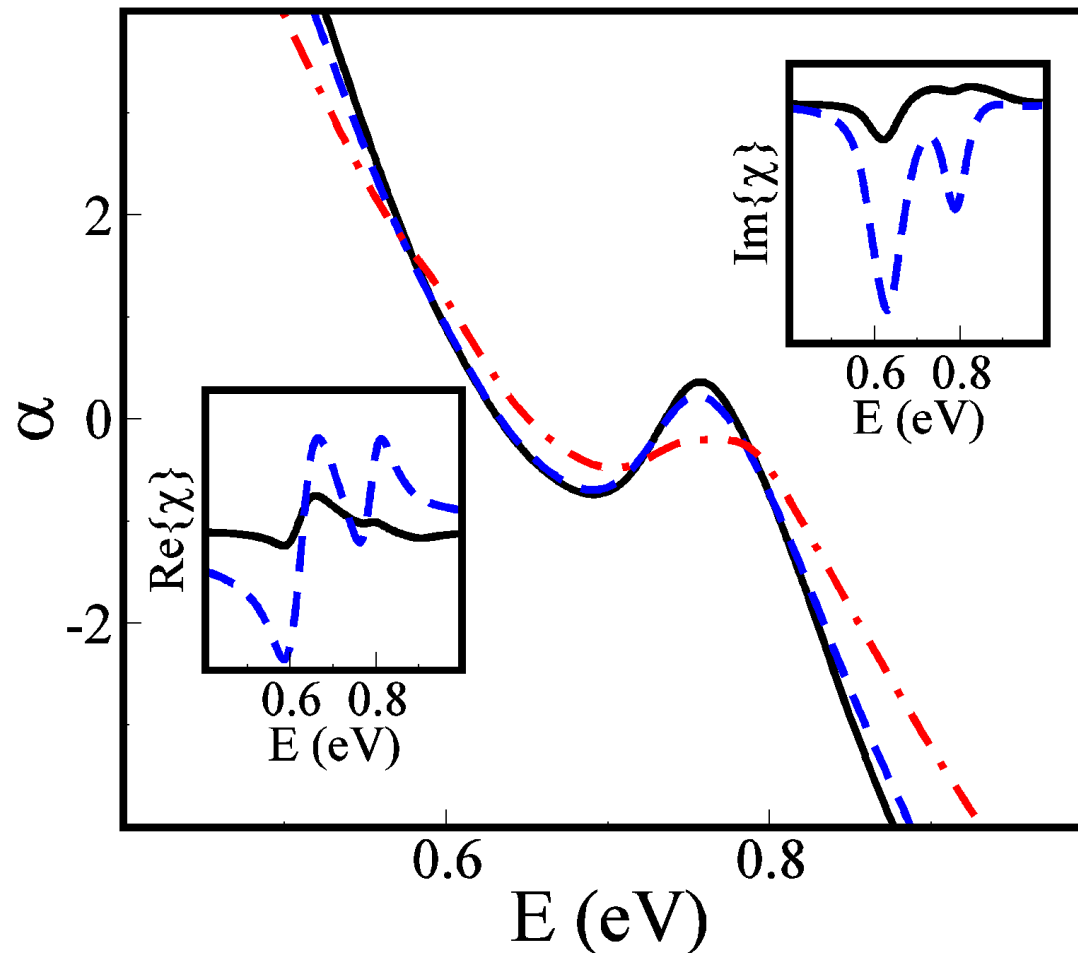
M. F. Pereira and S. Tomić, APL 98, 061101 (2011).

ISB Dispersive Gain Measured

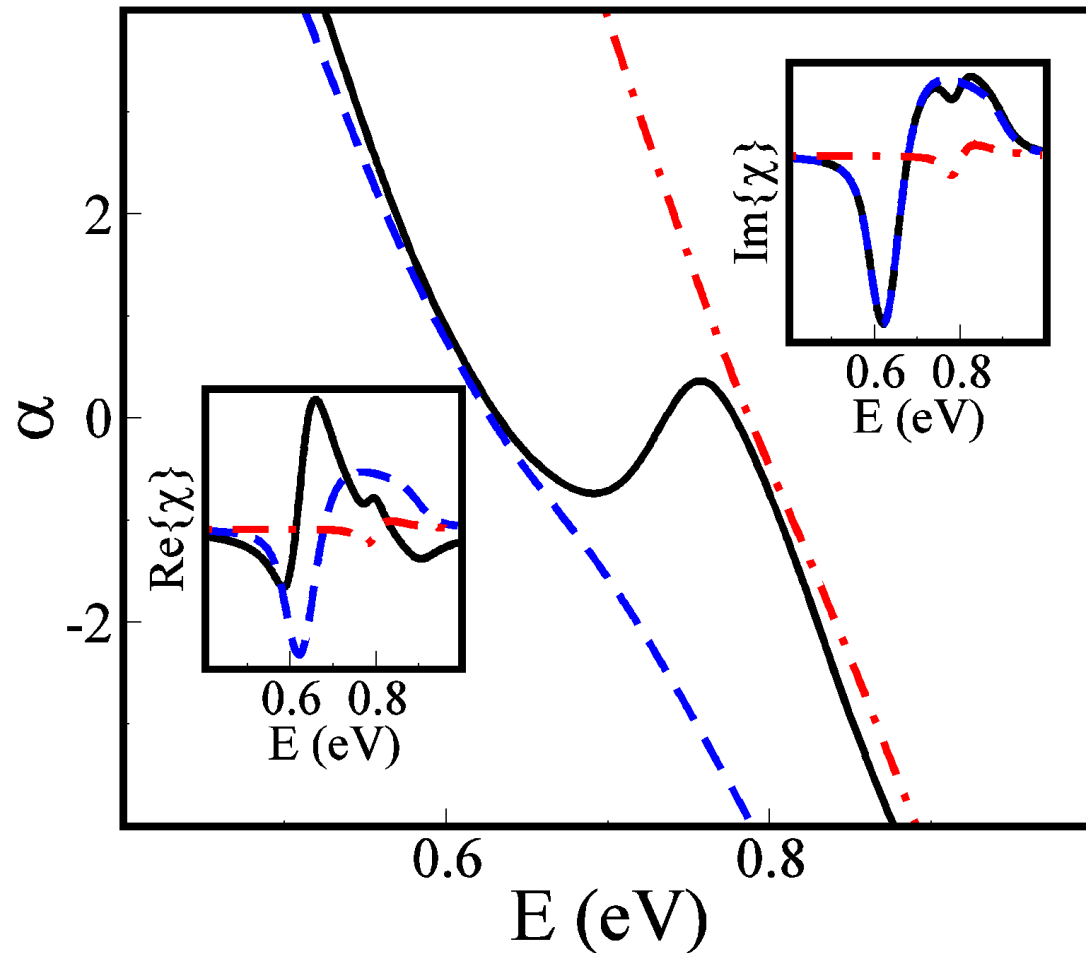
D.Revin et al. APL 92, 081110 (2008)



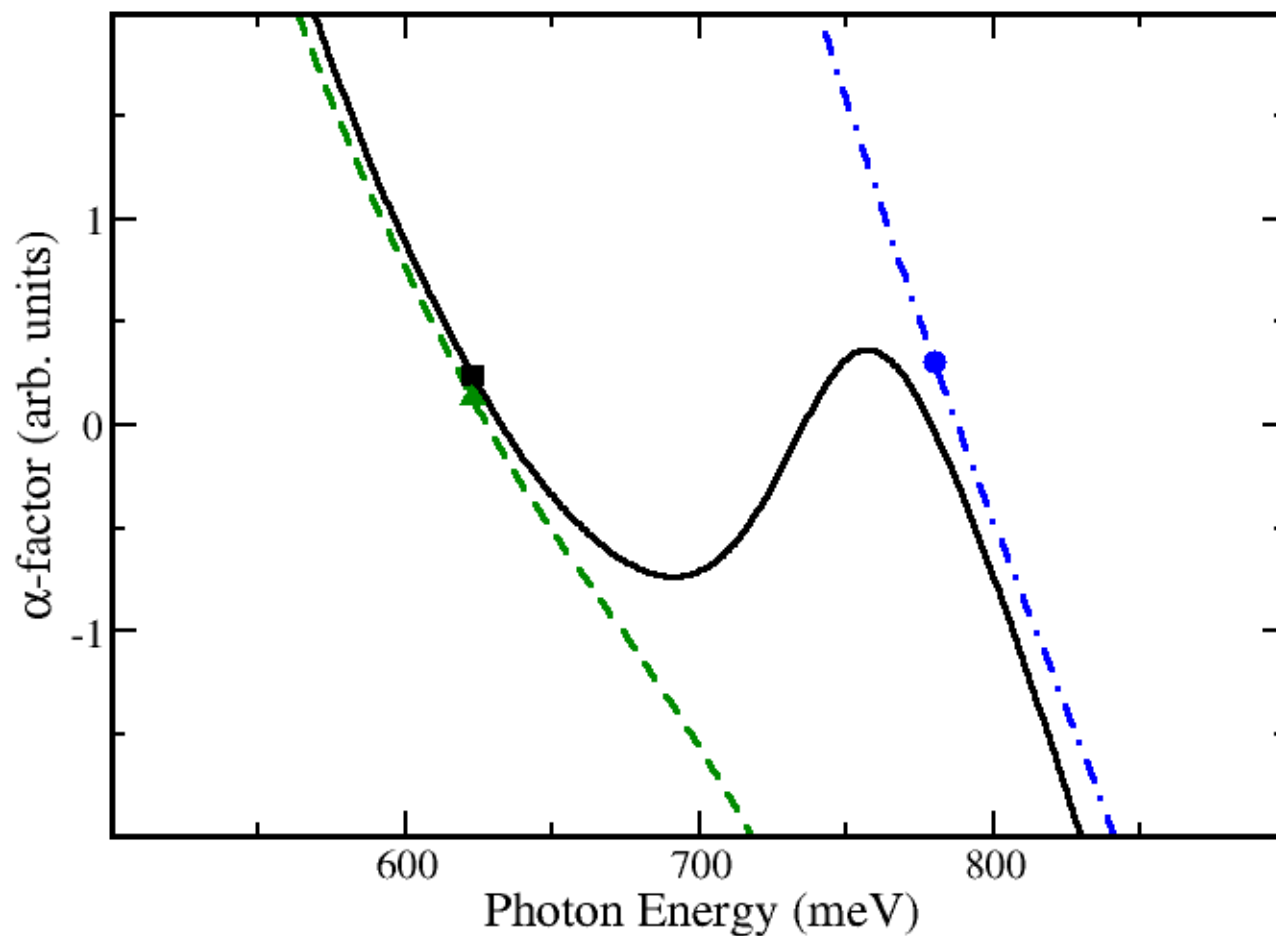
Evolution of α with increasing inversion



Combined effect of different transitions

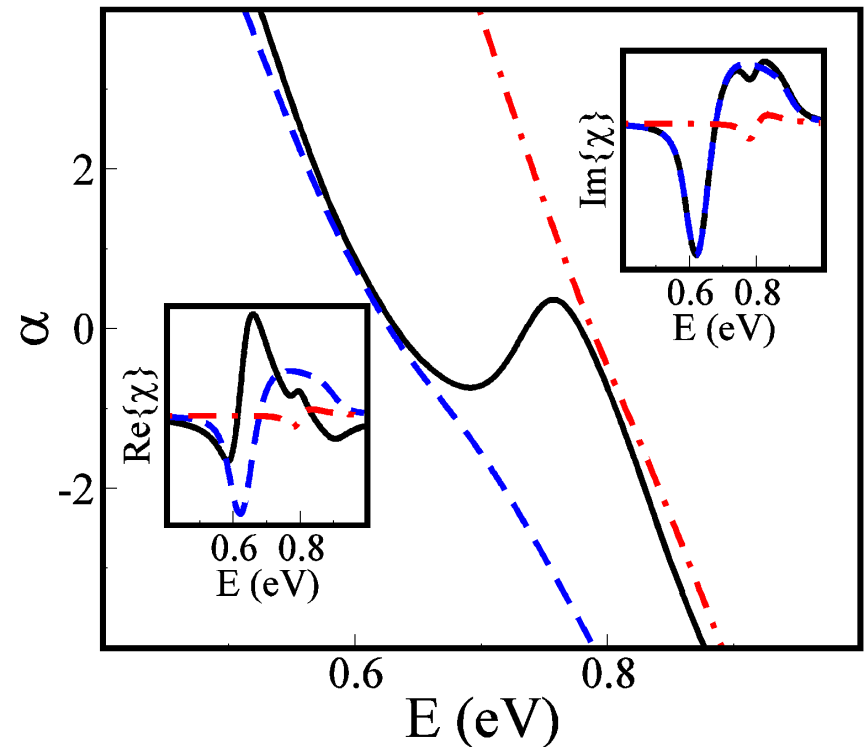
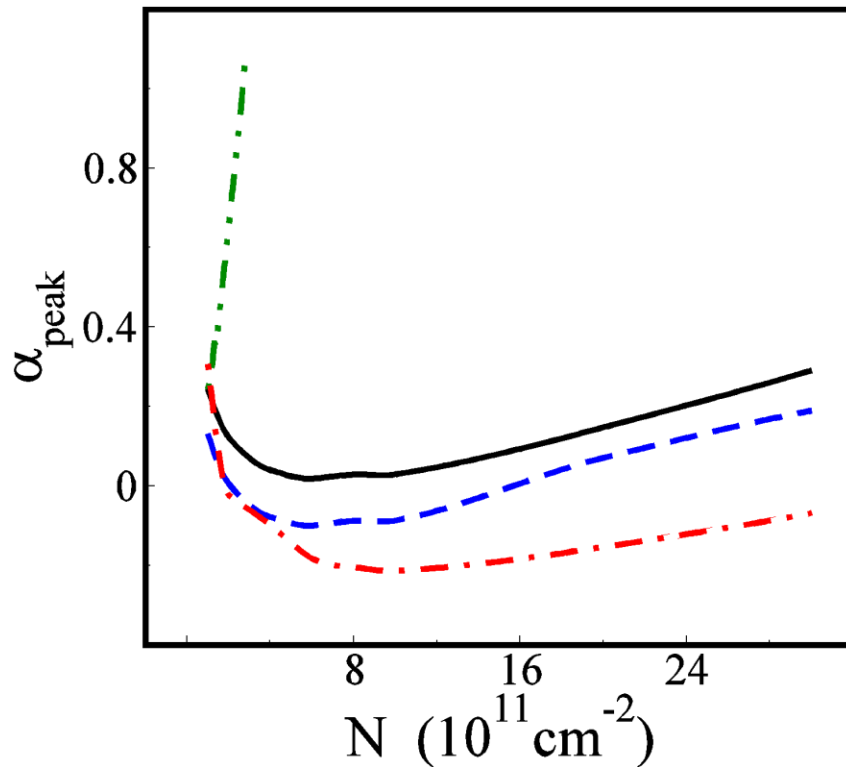


Combined effect of different transitions



Combined effect of different transitions

M.F. Pereira, Applied Physics Letters 109, 222102 (2016)



Summary

- This paper resolves the controversy created by intersubband α factors being measured with values ranging from -0.5 to 3 at peak gain, while they were expected to be zero.
- Counter rotating terms which are usually ignored because normally they do not affect the gain spectrum, are ultimately responsible for nonzero α factor at peak gain even without inclusion of nonparabolicity and manybody effects.
- For laser without inversion conditions, where the gain spectrum is typically dispersive instead of Lorentzian, the α factor at peak gain is a bit larger, but still within the range of values found for conventional intersubband lasers.

M.F. Pereira, *Applied Physics Letters* 109, 222102 (2016)